

PHYS 101

Ch. 6

Work and Kinetic Energy

Kinetic En. and the Work-En. Theo.

Example 1:

A particle moves 10 m in the positive x direction while being acted upon by a constant force $\vec{F} = (4\hat{i} + 4\hat{k})\text{N}$. The work done on the particle by this force is:

$$d = 10\hat{i} \quad (\text{positive-x})$$

$$(C) \quad F = 4\hat{i} + 4\hat{k}$$

- (A) 20 J
- (B) 10 J
- ~~(C) 40 J~~
- (D) -20 J

$$w = F \cdot d = 40 + 0 = 40 \text{ J}$$

Kinetic En. and the Work-En. Theo.

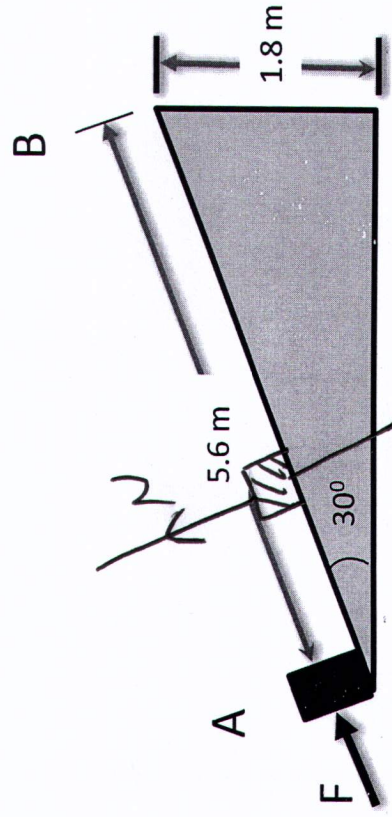
Example 2:

A force F causes the 2 kg box to slide up from point A to point B . The work done by the normal force on the box is:

Solution:

- (A) 49 J
- (B) 110.84 J
- ~~(C) Zero~~
- (D) 98 J

(C) $W_N = 0$ \perp



Kinetic En. and the Work-En. Theo.

Example 3:

Referring to Example 2, if $F=100\text{ N}$ and the distance between point A to point B is 5.6 m , the work done by the applied force on the box is:

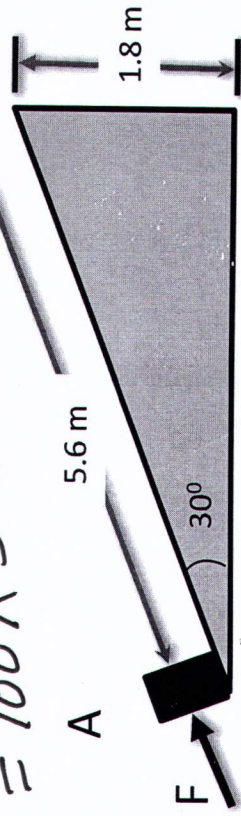
Solution:

- ~~(A) 560 J~~
- (B) -117.6 J
- (C) 98 J
- (D) 980 J

$$F = 100\text{ N}$$
$$(A) \quad d = 5.6\text{ m}$$

$$W = F \cdot d$$

$$W = 100 \times 5.6 = 560\text{ J}$$



Kinetic En. and the Work-En. Theo.

Example :

A man of mass 102 kg climbs a stair of 5 m height at constant speed. The work done by the man is:

Solution:

- (A) 9999.6 J
- (B) 510 J
- ~~(C)~~ 4998 J
- (D) 2499 J

$$\begin{aligned} m &= 102 \text{ kg} \\ d &= 5 \text{ m} \end{aligned}$$

(C)

$$W = mgd$$

$$W = 102 \times 9.8 \times 5$$

$$W = 4998 \text{ J}$$

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Kinetic En. and the Work-En. Theo.

Kinetic Energy

طاقة حركية

* **Kinetic energy** K is energy associated with the *state of motion* of an object. The faster the object moves, the greater is its kinetic energy. When the object is stationary, its kinetic energy is zero.

For an object of mass m whose speed v is

$$K = \frac{1}{2}mv^2$$

(kinetic energy).

- * m mass kg
- * v velocity m/s
- * K kinetic E J

* The SI unit of kinetic energy (and every other type of energy) is the joule (J),

$$1 \text{ joule} = 1 \text{ J} = 1 \text{ kg} \cdot \text{m}^2/\text{s}^2$$

Kinetic En. and the Work-En. Theo.

Example 4:

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An object that has kinetic energy must be :

Solution:

(A)

~~(A)~~ moving

(B) falling

(C) at rest

(D) non of these

Kinetic En. and the Work-En. Theo.

Example 5:

A moving particle of mass 2 kg, has kinetic energy of 10 J.
It speed is:

Solution:

- (A) 980 m/s
- (B) 9.8 m/s
- (C) 10 m/s
- (D) 3.16 m/s

$$K = \frac{1}{2} m U^2$$

(D)

$$10 = \frac{1}{2} \times 2 \times U^2$$

$$U = 3.16 \text{ m/s}$$

(D)

Kinetic En. and the Work-En. Theo.

Example 6:

A 4 kg cart starts up an incline with a speed of 3 m/s and comes to rest 2 m up the incline. The total work done on the cart is:

$$v_i = 3 \text{ m/s}$$

$$v_f = 0 \text{ m/s (rest)}$$

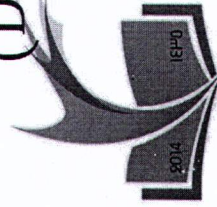
$$m = 4 \text{ kg}$$

(D)

- (A) -6 J
- (B) -8 J
- (C) -12 J
- (D) -18 J

$$W = \frac{1}{2} m (v_f^2 - v_i^2)$$

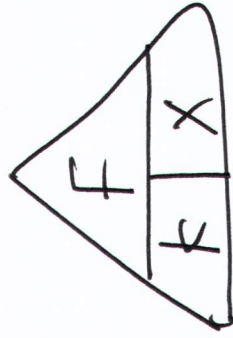
$$W = \frac{1}{2} \times 4 (0 - 9) \rightarrow W = -18 \text{ J}$$



Work and En. with Varying Forces

Example 8:

If the restoring force at distance 0.5 m is 15 N, then the work done in stretching spring a distance of 0.5 m is:



$$k = \frac{F}{x} \quad k = \frac{15}{0.5} = 30 \quad \text{(A)}$$

Solution:

- (A) -3.75 J
- (B) -6 J
- (C) -9 J
- (D) -12 J

$$W = -\frac{1}{2} k (\Delta x)^2$$

$$W = -\frac{1}{2} \times 30 (0.5)^2 = -3.75 \text{ J}$$

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Work and En. with Varying Forces

Example 9:

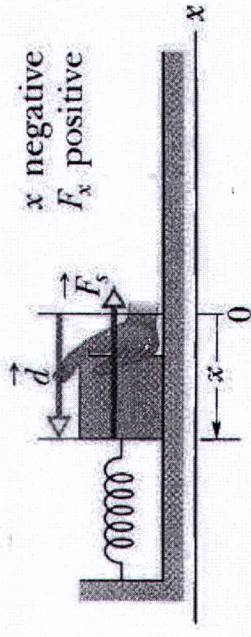
A force acts on a spring with length 30 cm. This force compressed it to be 25 cm. If the spring constant is 50 N/m, the work done by the spring is:

Solution:

- (A) -0.0625 J
- (B) -0.0825 J
- (C) -0.0932 J
- (D) -1.236 J

$$W = -\frac{1}{2} k(\Delta x)^2$$
$$W = -\frac{1}{2} \times 50(0.05)^2$$
$$W = -0.625 \text{ J}$$

(A)



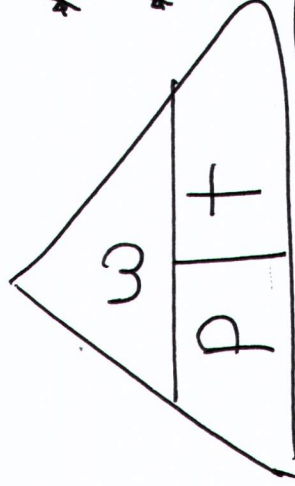
Power

Example 10:

If the work done on a particle is 32 J in 4 s. The power is:

Solution:

- (A) 36 W
- ~~(B) 8 W~~
- (C) 1 W
- (D) 6 W



(B)

$$\begin{aligned} * w &= 32 \text{ J} \\ * t &= 4 \text{ s} \end{aligned}$$

$$P = \frac{32}{4} = 8 \text{ watt}$$

Power

Example 11:

A box was pushed 3 m across the floor in 12 s by a horizontal force of 200 N. The amount of power is:

Solution:

- (A) 25 W
- (B) 100 W
- ~~(C) 50 W~~
- (D) 150 W

$$\begin{aligned} * F &= 200 \text{ N} \\ * d &= 3 \text{ m} \\ * t &= 12 \text{ s} \end{aligned}$$

(C)

$$P = \frac{w}{t} = \frac{f \cdot d}{t}$$

$$P = \frac{200 \times 3}{12} = 50 \text{ watt}$$