



## EE 202 – CIRCUIT THEORY II

Fall Semester 2017-2018

### Midterm Exam 1

Exam Date: Novemeber 06, 2017; Exam Duration: 90 minutes

Student's Full Name: \_\_\_\_\_

Student ID #: \_\_\_\_\_

Section #: 1053 Signature: \_\_\_\_\_

#### Instructions:

- Write your student ID number on the top of each page
- Write the solution in the space provided under each question
- Show all the details of your analysis and calculations

Question No.	Points Assigned	Points Awarded
1. [CO_6, PI_11_14, SO_11]	34	31
2. [CO_2, PI_1_27, SO_1]	33	19
3. [CO_5, PI_11_14, SO_11]	33	13
<b>Total</b>	<b>100</b>	<b>53</b>

Question 3 - (solution Continued)

Unit step: it's internal when we closed the ~~closed~~ circuit  
at the unit step mean it's very small ~~but~~ drop internal  
when we close the circuit to get the same value for  
(sources voltage or current) like

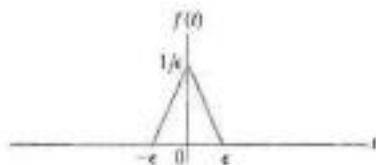


impulse functions: this function it's get the same value  
when we close the ~~open~~ circuit (so no unit step)

**Question 3**

Find the Laplace transform of (show steps)

- The derivative of unit step function (9 points)  $\rightarrow$  1
- coswt (9 points)
- What is the magnitude of  $f(t)$  when  $c=0$ ? (7 points)
- What is unit step and impulse functions? (8 points)



$$\frac{d}{ds} F(s) = 1$$

Solution



$$\int_{-\infty}^{\infty} F(s) \cdot ds$$

$$\Rightarrow 1 - 0 = 1$$



$$\frac{d}{ds} F(s) = 1$$

$$\frac{d}{ds} F(0) = 0$$

$$b) \cos \omega t = \frac{1}{(s+a)^2 \omega^2}$$

$$c) f(0) = \frac{1}{0} = \infty$$

$$b) P = |S| \cos \theta$$

$$Q = |S| \sin \theta$$

$$P = iV = (149,906 + j3,7474) \times (3) \\ = 449.718 + 11,241j$$

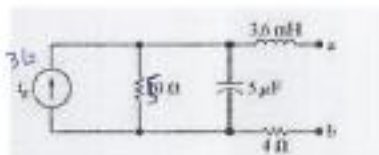
$$c) R_L = \sqrt{R_{th}^2 + (X_L + X_{th})^2}$$

$$d) P = \frac{1}{\eta} \frac{V}{R}$$

**Question 2**

The source current in the circuit shown is  $3 \cos 100t$  A as shown in figure, when value of resistor is taken 50 ohm instead of 20 ohm.

- What impedance should be connected across terminals a, b for maximum average power transfer? **(8 points)**
- What is the average power transferred to the impedance in (a)? **(9 points)**
- Assume that the load is restricted to pure resistance. What size resistor connected across a,b will result in the maximum average power transferred? **(9 points)**
- What is the average power transferred to the resistor in (c)? **(7 points)**



**Solution**

$$Z_L = Z_{Th}^*$$

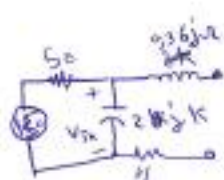
$$V = 3 \times 50 = 150 \text{ V}$$

$$\omega = 100 \Rightarrow X_L = \omega L = 0,36 \Omega \quad \left\{ \begin{array}{l} X_C = \frac{1}{\omega C} = 2000 \Omega \end{array} \right.$$

$$V_{Th} = \frac{2000j}{2000j + 50} \cdot 150 = 149,906 + 3,747j$$

$$\text{So } Z_{Th} = \frac{V_{oc}}{I} = \frac{149,906 + 3,747j}{3} = 49,968 + 1,24j$$

$$\Rightarrow Z_L = 49,968 - 1,24j$$



*Phasor Eq?*  
*Thevenin's Eq.*

$$\text{So } k_3 = k_1^* \Rightarrow k_3 = -15$$

$$\text{And } k_4 = k_2^* \Rightarrow k_4 = -15i$$

$$\Rightarrow \frac{60}{(s^2+4s+5)^2} = \frac{-15}{(s+2+i)^2} + \frac{15i}{(s+2+i)} + \frac{-15}{(s+2-i)^2} + \frac{-15i}{(s+2-i)}$$

So Laplace invers

$$\mathcal{L}^{-1}(F(s)) = -15t e^{-(2+i)t} + 15i e^{-(2+i)t} - 15t e^{-(2-i)t} - 15i e^{-(2-i)t}$$

~~poles: it's limit of  $F(s)$  when  $s \rightarrow \infty$~~

$$\lim_{s \rightarrow \infty} F(s)$$

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~~Zeros: it's limit of  $F(s)$  when  $s \rightarrow 0$~~

$$\lim_{s \rightarrow 0} F(s)$$