

**Question 2 (12 points)**

For the full-wave rectifier shown in Figure P2,  $R = 150 \Omega$ . A filter capacitor is connected in parallel with  $R$ . Assume  $V_y = 0.7$  V. The peak output voltage is to be 12 V and the ripple voltage is to be no more than 0.3 V. The input frequency is 60 Hz.

- Determine the required rms value of  $v_s$ .
- Determine the required filter capacitance value.
- Determine the peak current through the diodes.

**Solution**

a)  $v_s = v_m + 2V_y = 13.4V_p \quad \checkmark \quad v_{s\text{rms}} = 9.475V \quad \checkmark \quad 2$

b)  $V_y = \frac{V_m}{2fRC} \Rightarrow C = \frac{V_m}{2fRv_y} = 2222.2 \mu F \quad \checkmark \quad 4$

c)  $\star I_D = \frac{v_s - 2V_y}{R} = \frac{13.4 - 1.4}{150} = 0.08A$

Details: KVL In +ve cycle

$$v_s - v_2 - -v_o - V_y = 0$$

$$v_o = v_s - 2V_y$$

$$v_o = 13.4 - 2(0.7) = 12.$$

$$\therefore I_{D,(\text{f})} = \frac{12}{150} = 0.08$$

*wrong formula*

*y<sub>2</sub>*

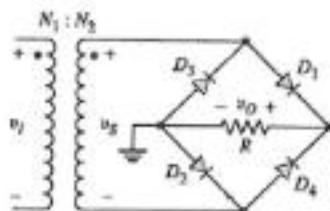


Figure P2

**Question 4 (25 points)**

For the common-gate circuit shown in Figure P4, the NMOS transistor parameters are:  $V_{TN} = 1$  V,  $K_n = 3$  mA/V<sup>2</sup>, and  $\lambda = 0$ .

- Draw the dc equivalent circuit.
- Calculate  $I_{DQ}$ ,  $V_{DSQ}$  and  $V_{GSA}$ .
- Draw the ac equivalent circuit.
- Calculate the small-signal parameters  $g_m$  and  $r_o$ .
- Draw the small-signal equivalent circuit.
- Derive and calculate the small-signal voltage gain  $A_v = V_o/V_i$ .

**Solution**

b)

$$I_{DQ} = K_n [V_{GS} - V_{TN}]^2 \quad \text{(assume int. region)} \quad \checkmark$$

KVL in  $L_1$ :

$$V^+ - I_D R_D - V_{DS} - I_D R_S - V^- = 0$$

$$5 - 5I_D - V_{DS} - 10I_D + 5 = 0$$

$$-15I_D + 10 = V_{DS} \quad \text{---} \quad \textcircled{3}$$

KVL in  $L_2$ :

$$-V_{GS} + -I_D R_S - V^- = 0$$

$$V_{GS} = -10I_D + 5 \quad \text{---} \quad \textcircled{2}$$

(22)

$$I_{DQ} = K_n [V_{GS}^2 - 2V_{GS}V_{TN} + V_{TN}^2]$$

$$I_{DQ} = K_n V_{GS}^2 - 2K_n V_{GS} V_{TN} + K_n V_{TN}^2$$

Substitute  $\textcircled{2}$  in  $\textcircled{3}$

$$I_{DQ} = K_n (-10I_{DQ} + 5)^2 - 2(-10I_{DQ} + 5)K_n V_{TN} + K_n V_{TN}^2$$

$$I_{DQ} = 3[100I_{DQ}^2 + 100I_{DQ} + 25] + 60I_{DQ} - 30 + 3$$

$$I_{DQ} = 300I_{DQ}^2 + 300I_{DQ} + 75 + 60I_{DQ} - 27$$

$$300I_{DQ}^2 + 241I_{DQ} - 27 = 0 \quad \text{---} \quad \textcircled{2}$$

$$I_{DQ} = -0.9 \text{ mA} \quad I_{DQ} = 0.09067 \text{ mA} \approx 0.1 \quad \checkmark$$

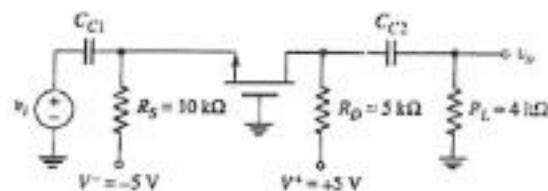
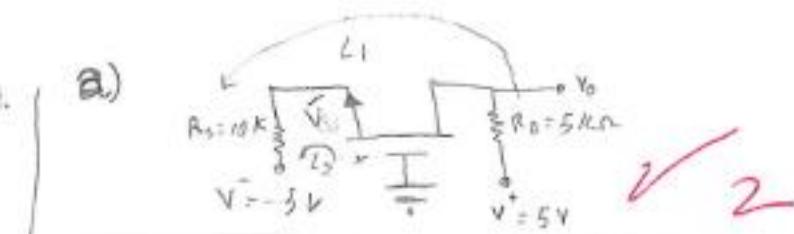


Figure P4

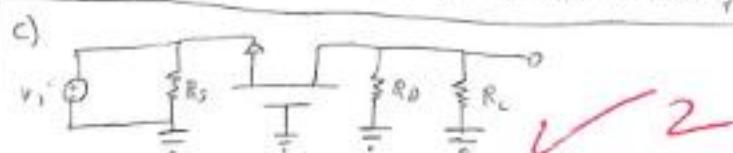


$$I_{DQ} = 0.1 \quad \text{---} \quad \textcircled{2}$$

$$\text{from } \textcircled{2}: V_{GS1} = -10(0.1) + 5 = +4 \text{ V} \quad \checkmark$$

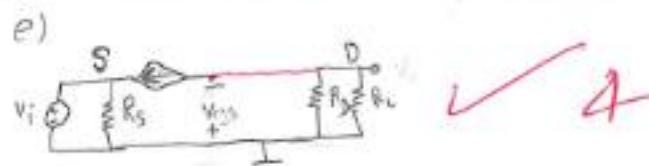
$$\text{from } \textcircled{3}: V_{DSQ} = -10(0.9) + 10 = -8.5 \text{ V} \quad \text{---} \quad \textcircled{2}$$

$$\text{check! } V_{DS(\text{min})} = V_{GS} - V_{TN} = +4 - 1 = +3 \text{ V} \quad \text{---} \text{ it is in int. region}$$



$$d) g_m = 2\sqrt{K_n I_{DQ}} = 1.09 \text{ mA/V} \quad \checkmark \quad \textcircled{2}$$

$$r_o = \frac{1}{\lambda I_{DQ}} = \infty \quad \checkmark \quad \textcircled{1}$$



$$f) V_o = -g_m V_{GS} R_D // R_L \quad \checkmark$$

$$V_{GS} = -V_i \quad \checkmark$$

$$A_v = \frac{V_o}{V_i} = g_m R_D // R_L \quad \text{because } g_m \ll 1 \quad \text{---} \quad \text{wrong}$$

$$A_v = -0.61 \quad \checkmark$$

**Question 3 (15 points)**

For the JFET circuit shown in Figure P3, the transistor parameters are  $I_{DSS} = 7 \text{ mA}$ , and  $V_p = 3 \text{ V}$ . Let  $R_1 + R_2 = 100 \text{ k}\Omega$ . Assume that  $I_{DQ} = 5.0 \text{ mA}$  and  $V_{SDQ} = 6 \text{ V}$ . Calculate

(a)  $V_{GSQ}$

(b)  $R_D$ ,  $R_1$  and  $R_2$ .

**Solution**

$$V_G = 12 \left( \frac{R_2}{R_1 + R_2} \right) \Rightarrow V_G = \frac{12 R_2}{100}$$

KVL in  $L_1$

$$V_{DD} - I_D R_S - V_G = 0$$

$$12 - (5 \times 0.3) - \frac{12 R_2}{100} = 0$$

$$(1) \quad 10.5 = \frac{12 R_2}{100}$$

$$12 R_2 = 1050$$

$$R_2 = \frac{1050}{12} = 87.5 \text{ k}\Omega$$

$$\rightarrow V_G = 12 \left( \frac{87.5}{100} \right) = 10.5 \text{ V}$$

KVL in  $L_2$

$$12 - I_D R_S - (V_{GSQ}) - I_D R_D = 0 \quad (1)$$

$$I_D = I_{DSS} \left[ 1 - \frac{V_{GS}}{V_p} \right]^2 \quad \text{THIS should be } V_{SDQ}$$

$$= 7 \left[ 1 - \frac{V_{GS}}{3} \right]^2$$

$$= 7 \left[ 1 - \frac{2}{3} V_{GS} + \frac{V_{GS}^2}{9} \right]$$

$$5 = 7 - \frac{14}{3} V_{GS} + \frac{2}{9} V_{GS}^2$$

$$\Rightarrow \frac{2}{9} V_{GS}^2 - \frac{14}{3} V_{GS} + 2 = 0$$

$$V_{GS1} = 5.5$$

$$V_{GS2} = 0.46$$

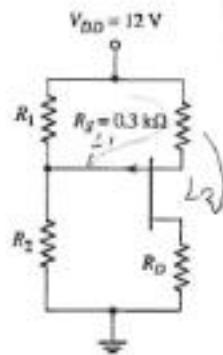


Figure P3

$$\therefore V_{GSQ} = 5.5 \text{ V}$$

substitute in (1):

$$12 - 5 \times 0.3 - 5.5 - 5 \times R_D = 0$$

$$= 5 = 5 R_D$$

$$\Rightarrow R_D = 1 \text{ k}\Omega$$

✓ because  $V_{GS}$  is wrong

$$V_G = 12 \left( \frac{R_2}{R_1 + R_2} \right)$$

$$V_G = 10.5, R_2 = 87.5$$

$$\Rightarrow 10.5 = 12 \left( \frac{87.5}{R_1 + 87.5} \right)$$

$$R_1 + R_2 = 100$$

$$\therefore R_1 = 100 - 87.5$$

$$R_1 = 12.5 \text{ k}\Omega$$

✓ 2

because  $V_{GS}$  is wrong

approach OR  
 drop value chosen!

correct answer 4

Question 2 (15 points)

Four infinite uniform sheets of charges are located in free space as given below:  
4 nC/m<sup>2</sup> at x = 3, -4 nC/m<sup>2</sup> at x = -3, 2 nC/m<sup>2</sup> at x = -1, -2 nC/m<sup>2</sup> at x = 5.  
Find E and D fields at point A(1, 2, -3), B(-2, 3, 5), and C(-3, 2, 4).

Solution

$$E_T = E_1 + E_2 + E_3 + E_4 \quad E \text{ for sheet of charge: } E = \frac{\rho_s}{2\epsilon_0} a_x$$

$$E_1 = 225.89 a_x \text{ V/m} \quad E_2 = -225 a_x$$

$$E_1 = \frac{4 \times 10^{-9}}{2 \times 8.854 \times 10^{-12}} \times \frac{1-3}{2} a_x = \cancel{225.89} \cancel{\frac{6}{4}} = \frac{-2}{2} a_x = -225 a_x \text{ V/m}$$

$$E_2 = \frac{-4 \times 10^{-9}}{2 \times 8.854 \times 10^{-12}} \times \frac{-1-(-3)}{4} a_x = -225 \times 1 a_x = -225 a_x \text{ V/m}$$

$$E_3 = \frac{2 \times 10^{-9}}{2 \times 8.854 \times 10^{-12}} \times \frac{1-(-1)}{2} = 112.9 a_x \text{ V/m}$$

(9) ~~8~~

$$E_4 = \frac{-2 \times 10^{-9}}{2 \times 8.854 \times 10^{-12}} \times \frac{1-5}{4} = -112 \times 1 a_x = 112 a_x \text{ V/m}$$

$$E_T \text{ at Point A} = -225.89 + 225 + 112.9 + 112.9 = \cancel{225.89} \cancel{+} \cancel{112.9} - 225.89 a_x \text{ V/m}$$

$$E_T \text{ at Point B} = E_1 + E_2 + E_3 + E_4 \quad B(-2, 3, 5)$$

$$E_1 = 225.89 \times \frac{-2-3}{5} a_x = -225.89 a_x$$

$$E_2 = -225.89 \times \frac{-2+3}{1} = 225.89 a_x$$

$$E_3 = 112.9 \times \frac{-2+1}{1} a_x = -112 a_x$$

$$E_4 = 112.9 \times \frac{-2-5}{7} = 112 a_x$$

$$E_T \text{ at Point B} = 0$$

Question 1 (15 points)

A vector  $\mathbf{F}$  is given as  $\mathbf{F} = 10 \mathbf{a}_r + 5 \mathbf{a}_\theta - 10 \mathbf{a}_\phi$ . Convert vector  $\mathbf{F}$  to rectangular coordinates at a point P (1,2,4).

Solution

$$\mathbf{F}_K = 10 \mathbf{a}_r \cdot \mathbf{a}_x + 5 \mathbf{a}_\theta \cdot \mathbf{a}_x - 10 \mathbf{a}_\phi \cdot \mathbf{a}_x$$

$$\mathbf{a}_r \quad \mathbf{a}_\theta \quad \mathbf{a}_\phi$$



$$F_x = 10 \mathbf{a}_r \cdot \mathbf{a}_x + 5 \mathbf{a}_\theta \cdot \mathbf{a}_x - 10 \mathbf{a}_\phi \cdot \mathbf{a}_x$$

$$F_x = 10 \mathbf{a}_r \cdot \mathbf{a}_z + 5 \mathbf{a}_\theta \cdot \mathbf{a}_z - 10 \mathbf{a}_\phi \cdot \mathbf{a}_z$$

$$x = r \sin \theta \cos \phi$$

$$y = r \sin \theta \sin \phi$$

$$z = r \cos \theta$$

IS

$$\Theta = \cos^{-1} \left( \frac{z}{r} \right) \rightarrow \sqrt{x^2 + y^2 + z^2}$$

$$\Phi = \tan^{-1} \left( \frac{y}{x} \right)$$

$$\Phi = \tan^{-1} \left( \frac{y}{x} \right) = 63.4^\circ$$

$$\begin{aligned} F_x &= 10 \sin \theta \cos \phi + 5 \cos \theta \cos \phi + 10 \sin \phi \\ &= 2.18 + 1.95 + 8.94 = 13.07 \mathbf{a}_x \end{aligned}$$

$$\Theta = \cos^{-1} \left( \frac{z}{\sqrt{x^2 + y^2 + z^2}} \right) = 29.2^\circ$$

$$\begin{aligned} F_y &= 10 \sin \theta \sin \phi + 5 \cos \theta \sin \phi - 10 \cos \phi \\ &= 4.36 + 3.9 - 4.48 = 3.78 \mathbf{a}_y \end{aligned}$$

$$\therefore \mathbf{F} = 13.07 \mathbf{a}_x - 3.78 \mathbf{a}_y + 6.29 \mathbf{a}_z$$

$$\begin{aligned} F_z &= 10 \cos \theta \sin \phi - 0 \\ &= 8.73 - 2.44 = 6.29 \mathbf{a}_z \end{aligned}$$



EE 282 – ELECTROMAGNETIC FIELD THEORY

Fall Semester 2016-2017

Q

Midterm Exam 1

Exam Date: 03/11/2016 ; Exam Duration: 90 minutes

Student's Full Name: Aamer Al-Khateeb

Student ID #: 342048 783 Section #: 2893 Signature: Signature

Instructions:

- Write your student ID number on the top of each page
- Write the solution in the space provided under each question
- Show all the details of your analysis and calculations

Question No.	Points Assigned	Points Awarded
1. [CO_1, PI_1_62, SO_1]	15	15
2. [CO_2, PI_1_46, SO_1]	15	09
3. [CO_3, PI_5_23, SO_5]	15	05
Total	45	29

Instructor's Full Name	Dr. Imdad Khan
Signature	



## EE 282 – ELECTROMAGNETIC FIELD THEORY

Fall Semester 2016-2017

### QUIZ 1

Grade

15

15

Name, Family Name : Aamer Al-Khateeb

ID No.: 342 048 783 Section No.: 2893 Signature:

Quiz Duration: 20 minutes.

Max Marks: 15

Instructions: Write "the correct" answer in the space provided under each question.

Question: [CO\_1, PI\_1\_62, SO\_1]

Three points are given in rectangular coordinate system as A(2,-3,5), B(-2,4,6) and C(1,0,-7).

1. Find the position vectors of the three points. (3)
2. Find the vector component of vector  $\vec{AB}$  in the direction of vector  $\vec{AC}$ . (6)
3. Find a unit vector which is normal to the surface containing the origin and the points A and B. (6)

Solution

$$1) \vec{P}_A = 2\vec{a}_x - 3\vec{a}_y + 5\vec{a}_z, \vec{P}_B = -2\vec{a}_x + 4\vec{a}_y + 6\vec{a}_z, \vec{P}_C = \vec{a}_x - 7\vec{a}_z \quad (3)$$

$$2) \vec{AB} = (-2-2)\vec{a}_x + (4+3)\vec{a}_y + (6-5)\vec{a}_z = -4\vec{a}_x + 7\vec{a}_y + \vec{a}_z \quad (6)$$

$$3) \vec{AC} = (1-2)\vec{a}_x + (0+3)\vec{a}_y + (-7-5)\vec{a}_z = -\vec{a}_x + 3\vec{a}_y - 12\vec{a}_z \quad (6)$$

to find the vector component of  $\vec{AB}$  in direction of  $\vec{AC}$  we do dot product

Between  $\vec{AB}$  and unit vector as:  $(\vec{AB} \cdot \vec{a}_{AC}) \vec{a}_{AC}$

$$\vec{a}_{AC} = \frac{\vec{AC}}{|\vec{AC}|} = \frac{-\vec{a}_x + 3\vec{a}_y - 12\vec{a}_z}{\sqrt{1^2 + 3^2 + 12^2}} = \frac{-\vec{a}_x}{\sqrt{154}} + \frac{3\vec{a}_y}{\sqrt{154}} - \frac{12\vec{a}_z}{\sqrt{154}}$$

$$\therefore \vec{AB} \cdot \vec{a}_{AC} = \frac{+4}{\sqrt{154}} + \frac{21}{\sqrt{154}} - \frac{12}{\sqrt{154}} = \frac{13}{\sqrt{154}} \rightarrow \text{then we multiply by } \vec{a}_{AC} \quad (6)$$

$$\left(\frac{13}{\sqrt{154}}\right) \vec{a}_{AC} = \boxed{\frac{-13}{154}\vec{a}_x + \frac{39}{154}\vec{a}_y - \frac{156}{154}\vec{a}_z} \rightarrow \text{equal}$$

$$= -0.08\vec{a}_x + 0.25\vec{a}_y - 1.01\vec{a}_z$$

→ Continue

**Question 6 (25 points)**

For the BJT transistor circuit shown in Figure P6, the parameters are  $\beta = 100$  and  $V_A = 100$  V. Find the dc voltages at the base and emitter terminals.

- Draw the dc equivalent circuit.
- Calculate  $I_{BO}$  and  $I_{CO}$ .
- Calculate  $R_C$  such that  $V_{CEQ} = 3.5$  V.
- Draw the ac equivalent circuit.
- Calculate the small-signal parameters  $r_o$ ,  $g_m$ , and  $r_i$ .
- Draw the small-signal equivalent circuit.
- Derive and calculate the small-signal voltage gain  $A_v = V_o/V_s$ .

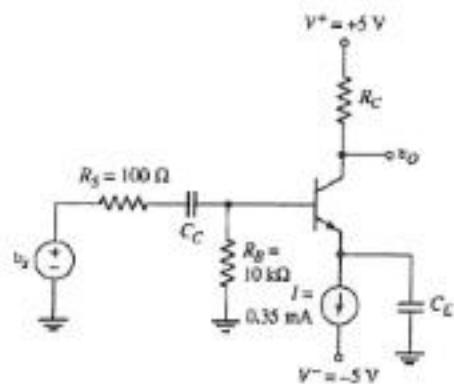


Figure P6

**Solution**

b)  $I_E = (1 + \beta) I_{BO}$

$I_{BO} = I_F / (1 + \beta) = 3.47 \mu A$  ✓ 3

$I_{CO} = \beta I_{BO} = 0.347 \text{ mA}$  ✓ 3

c)  $V_{BE}$  in L1:

$V^+ - I_C R_C - V_{EC} - V^- = 0$

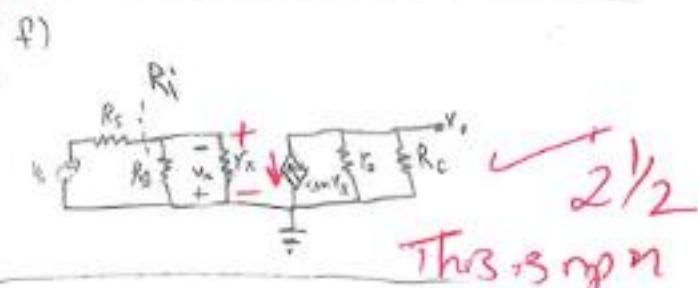
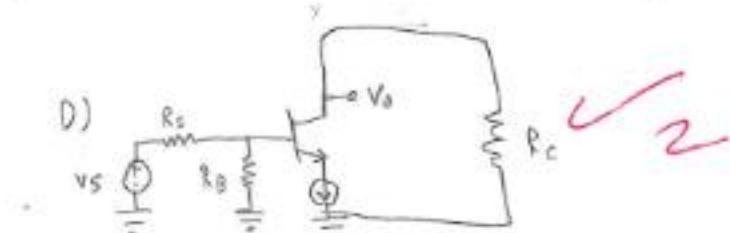
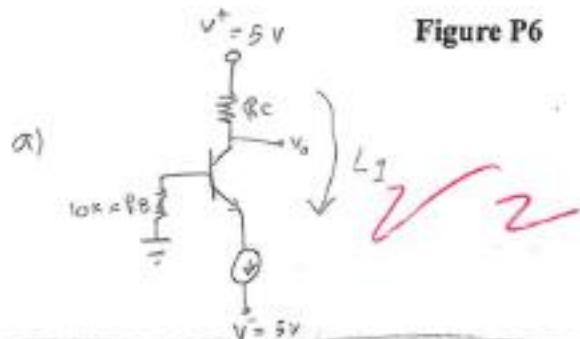
$R_C = \frac{V^+ - V_{EC}}{I_C} = 18.73 \text{ k}\Omega$  ✓ 2  
 calc. mistake

e)  $r_R = \frac{\beta V_T}{I_{CO}} = 7.5 \text{ k}\Omega$  ✓ 1

$g_m = \frac{I_{CO}}{V_T} = 13.35 \text{ mA/V}$  ✓ 1

$r_o = \frac{V_A}{I_{CO}} = \frac{100}{0.347} = 288 \text{ k}\Omega$  ✓ 1

23



g)  $V_o = r_{in} v_e (r_o // R_C)$

$v_e = -v_i \left( \frac{R_i}{R_i + R_S} \right)$  ✓  $R_i = r_R // R_B = 4.29 \text{ k}\Omega$

$A_v = \frac{V_o}{V_i} = -g_m (r_o // R_C) \left( \frac{R_i}{R_i + R_S} \right) = -229.4$  ✓ 5 1/2  
 (Not logical answer)

but if I assume  $R_S = 100 \text{ k}\Omega$ ,  $A_v$  will be = -9.66  
 which seems logical.

**Question 5 (15 points)**

For the BJT transistor circuit shown in Figure P5, the parameters are  $\beta = 120$  and  $V_{EB(on)} = 0.7 \text{ V}$ .

- Calculate  $I_{BQ}$ ,  $I_{CQ}$  and  $V_{ECQ}$ .
- Sketch the dc load line indicate the Q-point.

**Solution**

KVL in L1 yields:

$$a) I_B = \frac{V^+ - V_{EB}}{R_B} = 17.2 \mu\text{A} \quad \checkmark \quad 1$$

$$I_{CQ} = \beta I_{BQ} = 2.064 \text{ mA} \quad \checkmark$$

$$I_{EQ} = (1 + \beta) I_{BQ} = 2.0812 \text{ mA} \quad 2$$

KVL in L2:

$$V^+ - V_{EC} - I_C R_C - V^- = 0$$

$$5 - V_{EC} - (2.064 \times 1.5) + 5 = 0$$

$$V_{EC} = 10 - 3.096 = \underline{\underline{6.904}} \quad \checkmark \quad 4$$

LL eq:  $V_{EC} = 10 - 1.5 I_C$

(15)

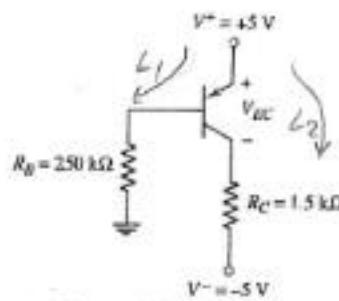
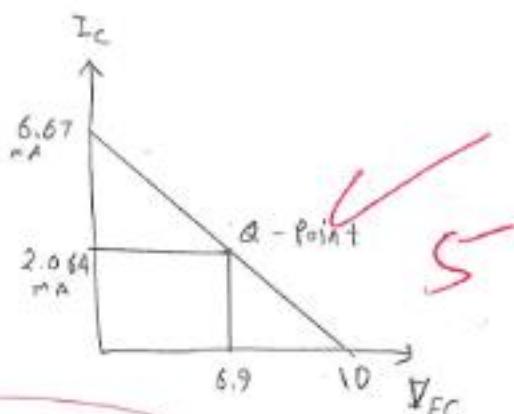


Figure P5





**EE 212 - ELECTRONICS II**

Fall Semester 2016-2017

**Final Exam**

**Exam Date: January 15, 2017; Exam Duration: 120 minutes**

**Student's Full Name:** Aamer Al-Khatib

**Student ID #:** 342048783 **Section #:** 2888 **Signature:** Qasim

**Instructions:**

- Write your student ID number on the top of each page
- Write the solution in the space provided under each question
- Show all the details of your analysis and calculations

Question No.	Points Assigned	Points Awarded
1. [CO_1, PI_1_45, SO_1]	8	8
2. [CO_3, PI_5_51, SO_5]	12	8.5
3. [CO_8, PI_5_52, SO_5]	15	11
4. [CO_10, PI_5_54, SO_5]	25	22
5. [CO_5, PI_5_49, SO_5]	15	15
6. [CO_7, PI_5_53, SO_5]	25	23
Total	100	87.5 / 100

Instructor's Full Name	Prof. Kemal Fidanboylu
Signature	

Question 3 (15 points)

- Derive Maxwell's first equation. What is the integral form of Maxwell's first equation? (10)
- Given  $D = 3x^3yz \mathbf{a}_x + x^2y^2z^2 \mathbf{a}_y - 2xz^3 \mathbf{a}_z \text{ C/m}^2$ , find the divergence of  $D$  and the volume charge density at point P(2,3,5). (5)

Solution

1)  $\oint \operatorname{Div} \cdot D = Q$

2)  $D = 3x^3yz \mathbf{a}_x + x^2y^2z^2 \mathbf{a}_y - 2xz^3 \mathbf{a}_z$

$\operatorname{div} D =$

$$\frac{\partial D_x}{\partial x} = 9x^2yz$$

$$\frac{\partial D_y}{\partial y} = 2x^2y^2z^2$$

$$\frac{\partial D_z}{\partial z} = -6xz^2$$

$$\therefore \operatorname{div} D = 9x^2yz + 2x^2y^2z^2 - 6xz^2$$

$P_V = \operatorname{div} D$

$$P_V \text{ at } P(2,3,5) = (9 \times 2^2 \times 3 \times 5) + (2 \times 2^2 \times 3 \times 5^2) + (-6 \times 2 \times 5^2)$$
$$= 540 + 600 + -300 = 840 \text{ C/m}^3$$

$$\therefore P_V = 840 \text{ C/m}^3$$