

# **Chapter 5**

## **Gases**

**Dr. Dalal Alezi**  
**dalezi@kau.edu.sa**

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# Chapter 5: Gases

Gas Units

$$1 \text{ atm} = 760 \text{ mmHg (torr)} = 101 \text{ kPa}$$

$$\begin{aligned} 1 \text{ atm} &= 760 \text{ mmHg} \\ 1 \text{ atm} &= 76 \text{ cmHg} \\ 1 \text{ atm} &= 1.01325 \times 10^2 \text{ kPa} \\ 1 \text{ torr} &= 1 \text{ mmHg} \end{aligned}$$

Gas laws

Boyle's Law  
 $P_1V_1 = P_2V_2$

Avogadro's Law  
 $V_1n_2 = V_2n_1$

Ideal gas equation

Charles's & Gay-Lussac's  
 $V_1T_2 = V_2T_1$

Combined Gas Equation

$$\frac{P_1V_1}{n_1T_1} = \frac{P_2V_2}{n_2T_2}$$

Density and MM of gases

$$PV = nRT$$

(STP condition)

Gas Stoichiometry

Determine empirical and molecular formula

Dalton's Law

$$P_{\text{total}} = P_1 + P_2 \dots$$
$$P_A = P_t X_A$$

Collecting a Gas over Water

- Elements that exist as gases at 25 °C and 1 atm (blue boxes)

1A																		8A
H																		He
Li	Be											B	C	N	O	F		Ne
Na	Mg											Al	Si	P	S	Cl		Ar
		3B	4B	5B	6B	7B	8B			1B	2B							
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br		Kr
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I		Xe
Cs	Ba	La	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At		Rn
Fr	Ra	Ac	Rf	Db	Sg	Bh	Hs	Mt	Ds	Rg								

- Noble gases are monoatomic, e.g. He, Ne, Ar
- Other gases are diatomic, e.g. H<sub>2</sub>, N<sub>2</sub>, O<sub>2</sub>

## Pressure units

$$1 \text{ atm} = 760 \text{ mmHg}$$

$$1 \text{ atm} = 76 \text{ cmHg}$$

$$1 \text{ atm} = 1.01325 \times 10^5 \text{ Pa}$$

$$1 \text{ atm} = 1.01325 \times 10^2 \text{ kPa}$$

$$1 \text{ torr} = 1 \text{ mmHg}$$

# Convert 688 mmHg to atmosphere?

$$1 \text{ atm} = 760 \text{ mmHg}$$

$$1 \text{ atm} \quad \rightarrow \quad 760 \text{ mmHg}$$

$$? \text{ atm} \quad \rightarrow \quad 688 \text{ mmHg}$$

$$(1 \times 688) / 760 = 0.905 \text{ atm}$$

What is the pressure in kPa of 732 mmHg?

$$760 \text{ mmHg} = 1.01325 \times 10^2 \text{ kPa}$$

$$760 \text{ mmHg} \rightarrow 1.01325 \times 10^2 \text{ kPa}$$

$$732 \text{ mmHg} \rightarrow ? \text{ kPa}$$

$$= 97.6 \text{ kPa}$$

(5.19 book) A gas sample occupying a volume of 725 ml at a pressure of 0.97 atm is allowed to expand at constant temperature until its pressure reaches 0.541 atm. What is its final volume?

$$V_1 = 725 \text{ ml} \quad P_1 = 0.97 \text{ atm} \quad P_2 = 0.541 \text{ atm} \quad V_2 = ?$$

$$P_1 V_1 = P_2 V_2 \quad V_2 = P_1 V_1 / P_2$$

$$V_2 = 0.97 \times 725 / 0.541 = 1299 \text{ ml}$$

(5.21 book) the volume of a gas is 5.8 L, measured at 1 atm. What is the pressure of the gas in mmHg if the volume is changed to 9.65 L? ( the temperature remain constant)

$$V_1=5.8 \text{ L} \quad P_1=1\text{atm} \quad V_2= 9.65 \text{ L} \quad P_2=? \text{ mmHg}$$

$$P_1V_1=P_2V_2 \quad \Longrightarrow \quad P_2= P_1V_1 / V_2$$

$$P_2= 1 \times 5.8 / 9.65 = 0.601 \text{ atm}$$

$$P_2=0.601 \times 760 = 456.76 \text{ mmHg}$$



(5.23) A 36.4 L volume of methane gas is heated from 25 °C to 88°C at constant pressure . What is the final volume of the gas?

$$V_1=36.4 \text{ L} \quad T_1=25+273=\underline{298} \text{ K} \quad T_2=88+273=361 \text{ K} \quad V_2=?$$

$$V_1T_2=V_2T_1 \implies V_2 = V_1T_2/\underline{T_1}$$

$$V_2=36.4 \times 361 / 298 = 44.09 \text{ L}$$

A student collects 125 ml sample of hydrogen gas. Later, the sample is found to have a volume of 128.6 ml at 26°C, at what temperature (in C) the sample was collected?

$$V_1=125\text{ml} \quad T_1=? \quad V_2=128.6 \text{ ml} \quad T_2= 26+273=299 \text{ K}$$

$$V_1T_2=V_2T_1 \implies T_1 = V_1T_2 / \underline{V_2}$$

$$T_1 = 125 \times 299 / 128.6 = 290.6 \text{ K}$$

$$T_1 = 290.6 - 273 = 17.6 \text{ }^\circ\text{C}$$

What pressure in atmosphere will 18.6 mol methane exert when its compressed in 12 L tank at temperature 45°C?

P=?      n=18.6 mol      V=12 L      T=45+273=318 K      R=0.0821 atm.L/mol.K

$$PV=nRT$$

$$P=nRT/V$$

$$P=18.6 \times 0.0821 \times 318 / 12 = 40.5 \text{ atm}$$

What volume does 0.056 mol of H<sub>2</sub> gas occupy at 25°C and 1.11 atm pressure ?

V=?

n=0.056 mol

T=25+273=298 K

P=1.11 atm

**R=0.0821 atm.L/mol.K**

$$PV=nRT$$

$$V = nRT / P$$

$$V = 0.056 \times 0.0821 \times 298 / 1.11 = 1.23 \text{ L}$$

What volume is occupied by 1 g H<sub>2</sub>O vapor at temperature 134°C and pressure of 0.0552 atm?

$$V=? \quad m=1 \text{ g} \quad T=134+273=407 \text{ K} \quad P=1.11 \text{ atm}$$

$$n=m/M \quad \longrightarrow \quad n=1/18.016=0.056 \text{ mol}$$

$$PV=nRT$$

$$V = nRT / P$$

$$V=0.056 \times 0.0821 \times 407 / 0.0552 = 33.9 \text{ L}$$

How many moles are in 148 mL gas at 13°C and pressure 107 kPa?

$$n=? \quad V=148\text{ml}/1000=0.148 \text{ L} \quad T=13+273=286 \text{ K}$$

$$P=107 \text{ kPa} / 1.013 \times 10^2 = \underline{1.05} \text{ atm}$$

$$PV=nRT$$

$$n = PV/RT$$

$$n= 1.05 \times 0.148 / 0.0821 \times 286 = 6.6 \times 10^{-3} \text{ mol}$$

A sample of nitrogen monoxide has a volume 72.6 ml at temperature 16°C and a pressure 104.1 kPa. What volume the sample will occupy at temperature 24 °C and pressure 99.3 kPa?

In this Question the sample has **n is constant**

$$V_1=72.6 \text{ mL} \quad P_1=104.1 \text{ kPa} \quad T_1= 16+273=289 \text{ K}$$

$$V_2=\underline{?} \quad P_2= 99.3 \text{ kPa} \quad T_2= 24+273=297 \text{ K}$$

$$\frac{P_1 V_1}{n_1 T_1} = \frac{P_2 V_2}{n_2 T_2}$$

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

$$\longrightarrow V_2 = P_1 V_1 T_2 / P_2 T_1$$

$$V_2 = 104.1 \times 72.6 \times 297 / 99.3 \times 289$$

$$V_2 = 78.2 \text{ mL}$$

A balloon was inflated with 2.42 L of helium gas at temperature 27°C. Later, the volume of balloon changed to 2.37L at temperature 19°C and pressure 99.7 kPa. What was the pressure when the balloon was inflated?

$$V_1 = 2.42 \text{ L}$$

$$T_1 = 27 + 273 = 300 \text{ K}$$

$$P_1 = ?$$

$$V_2 = 2.37 \text{ L}$$

$$T_2 = 19 + 273 = 292 \text{ K}$$

$$P_2 = 99.7 \text{ kPa}$$

$$\frac{P_1 V_1}{n_1 T_1} = \frac{P_2 V_2}{n_2 T_2}$$

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

$$\Rightarrow P_1 = P_2 V_2 T_1 / V_1 T_2$$

$$P_1 = 99.7 \times 2.37 \times 300 / 2.42 \times 292 = 100.3 \text{ kPa}$$



What is the final volume of 5 L gas when the final pressure become double the original at constant temperature?

$$V_1 = 5L$$

$$V_2 = \underline{\underline{?}}$$

$$P_1$$

$$P_2 = 2 P_1$$

$$P_1 V_1 = P_2 V_2$$

$$P_1 \times 5 = 2P_1 \times V_2$$

$$V_2 = 5P_1 / 2P_1$$

$$V_2 = 5/2 = 2.5 L$$

Ans: 2.5 L

Calculate the density of sulfur dioxide (SO<sub>2</sub>) in grams per liter (g/L) at 2.3 atm and 60 C°

$$d = ?? \text{ g/L}$$

$$P = 2.3 \text{ atm}$$

$$T = 60 + 273.15 = 333.15 \text{ K}$$

$$M = 32.06 + (2 \times 16) = 64.06 \text{ g/mol}$$

$$d = \frac{PM}{RT}$$

$$d = \frac{2.3 \times 64.06}{0.082 \times 333.15}$$

$$d = 5.39 \text{ g/L}$$

Ans: 5.39 g/L

Calculate the density of gas in grams per liter (g/L) at 1.5 atm and 30 °C. Assuming that we have 4.5 mole of this gas. If you know that the mass of this gas is 126 g.

$$d = ?? \text{ g/L}$$

$$P = 1.5 \text{ atm}$$

$$T = 30 + 273.15 = 303.15 \text{ K}$$

$$M = \frac{m}{n} = \frac{126}{4.5} = 28 \text{ g/mol}$$

$$d = \frac{PM}{RT}$$

$$d = \frac{1.5 \times 28}{0.082 \times 303.15}$$

$$d = 1.69 \text{ g/L}$$

Ans: 1.69 g/L

Which of these gases will have the greatest density at the same specified temperature and pressure?

A) O<sub>2</sub>    B) Kr    C) CO    D) C<sub>2</sub>H<sub>6</sub>

The density of a gas is directly proportional to its molar mass

كثافة الغاز تتناسب طرديا مع كتلته المولارية

$$d \propto M$$

Gases	Molar mass
O <sub>2</sub>	2×16=32 g/mol
Kr	83.8 g/mol
CO	12+16=28 g/mol
C <sub>2</sub> H <sub>6</sub>	2×12+6×1.008= 30.05 g/mol

What is the molar mass of Freon-12 gas if its density is 11.19 g/L at 2.3 atm and 30 °C?

$$M = ??$$

$$d = 11.19 \text{ g/L}$$

$$P = 2.3 \text{ atm}$$

$$T = 30 + 273.15 = 303.15 \text{ K}$$

$$M = \frac{dRT}{P}$$

$$M = \frac{11.19 \times 0.082 \times 303.15}{2.3}$$

$$M = 120.94 \text{ g/mol}$$

Ans: 120.94 g/mol

Calculate the volume of CO(in L) produced from 4.2L of (O<sub>2</sub>) at the same T & P



	Volume of CO		Volume of O <sub>2</sub>
من المعادلة الكيميائية	2L	←	3L
من المسألة	??L	←	4.2L

$$V_{\text{CO}} = \frac{4.2 \times 2}{3} = 2.8 \text{ L}$$

Ans: 2.8 L

What volume of CO<sub>2</sub> gas at 800 torr and 565 K could be produced by the reaction of 62 g of CaCO<sub>3</sub> according to the equation?



	moles of CO <sub>2</sub>	moles of CaCO <sub>3</sub>
من المعادلة الكيميائية	1	1
من المسألة	??	$\frac{62}{40.08 + 12 + (3 \times 16)} = 0.62$

$$n_{\text{CO}_2} = 0.62 \text{ mol}$$

$$P = 800 \text{ torr} / 760 = 1.05 \text{ atm}$$

$$T = 565 \text{ K}$$

$$V_{\text{CO}_2} = ?$$

$$PV = nRT$$

$$1.05 \times V = 0.62 \times 0.082 \times 565$$

$$V = 27.35 \text{ L}$$

Ans: 27.35 L

A mixture of two gases has a total pressure of 1852 mmHg at 21°C. The mixture is analyzed and is found to contain 6.5 mol CO, and 3.6 mol He. What is the partial pressure of He?

$$P_{He} = P_T X_{He}$$

$$X_{He} = \frac{n_{He}}{n_T}$$

$$P_T = 1852 \text{ mmHg}, \quad n_{CO} = 6.5 \text{ mol}, \quad n_{He} = 3.6 \text{ mol}, \quad n_T = n_{CO} + n_{He} = 6.5 + 3.6 = 10.1 \text{ mol}$$

$$P_{He} = 1852 \times \frac{3.6}{10.1}$$

$$P_{He} = 660.1 \text{ mmHg}$$

Ans: 660.1 mmHg



A mixture of two gases has a total pressure of 5 atm at 25°C. The mixture is analyzed and is found to contain 500 g Kr, and 50 g He. What is the partial pressure of Kr?

$$P_{Kr} = P_T X_{Kr}$$

$$X_{Kr} = \frac{n_{Kr}}{n_T}$$

$$P_T = 5 \text{ atm}, \quad n_{Kr} = \frac{500}{83.8} = 5.97 \text{ mol}, \quad n_{He} = \frac{50}{4} = 12.5 \text{ mol},$$

$$n_T = n_{Kr} + n_{He} = 5.97 + 12.5 = 18.47 \text{ mol}$$

$$P_{Kr} = 5 \times \frac{5.97}{18.47}$$

$$P_{Kr} = 1.6 \text{ atm}$$

Ans: 1.6 atm

A sample of oxygen gas was collected over water at 30°C and 701 mmHg. The volume of the container was 5.66 L. Calculate the mole of O<sub>2</sub> collected. (Vapor pressure of water = 31.82 mmHg at 30°C.)

$$T=30+273.15=303.15\text{K}$$

$$P_T=701\text{ mmHg} \quad P_{\text{H}_2\text{O}}=31.82\text{ mmHg} \quad P_{\text{O}_2}=P_T - P_{\text{H}_2\text{O}} = 701 - 31.82=669\text{mmHg}/760 \\ =0.88\text{ atm}$$

$$V=5.66\text{L} \quad n_{\text{O}_2}=??$$

$$PV=\underline{nRT}$$

$$0.88 \times 5.66 = n \times 0.082 \times 303.15$$

$$n=0.2\text{ mol}$$

Ans: 0.2 mol

A sample of hydrogen gas was collected over water at 30°C and 2 atm. The volume of the container was 100 ml . Calculate the mass of H<sub>2</sub>(g) collected. (Vapor pressure of water = 0.04 atm at 30°C.)

$$T=30+273.15=303.15\text{K}$$

$$P_T= 2 \text{ atm} \quad P_{\text{H}_2\text{O}}=0.04 \text{ atm} \quad P_{\text{H}_2}= P_T -P_{\text{H}_2\text{O}} = 2 - 0.04=1.96 \text{ atm}$$

$$V=100/1000=0.1\text{L}$$

$$m=??$$

$$PV=\underline{nRT}$$

$$1.96 \times 0.1 = n \times 0.082 \times 303.15$$

$$n=7.88 \times 10^{-3} \text{ mol}$$

$$n=\frac{m}{M}$$

$$7.88 \times 10^{-3} = \frac{m}{(2 \times 1.008)}$$

$$m=0.016 \text{ g}$$

Ans: 0.016 g

A sample of hydrogen gas was collected over water occupied 1.2 L at 288.15K and pressure 500 torr. What volume would H<sub>2</sub> occupy if were dry at STP? The pressure of water at 288.15K is 12.79 torr

$$V_1=1.2\text{L}$$

$$T_1=288.15\text{K}$$

$$P_T= 500 \text{ torr}, P_{\text{H}_2\text{O}}=12.79 \text{ torr}, P_1= P_T - P_{\text{H}_2\text{O}} = 500 - 12.79=487.21 \text{ torr}/760=0.64\text{atm}$$

$$V_2=??$$

$$\text{STP} \rightarrow P_2=1 \text{ atm} \quad T_2=273.15\text{K}$$

$$\frac{P_1V_1}{T_1} = \frac{P_2V_2}{T_2}$$

$$\frac{0.64 \times 1.2}{288.15} = \frac{1 \times V_2}{273.15}$$

$$V_2=0.73 \text{ L}$$

Ans: 0.73 L

A sample of hydrogen gas was collected over water occupied 4.0 L at 288.15K and pressure 0.87 atm. What volume would H<sub>2</sub> occupy if were dry at 400 K and 1.01 atm? The pressure of water at 288.15K is 0.017 atm.

$$V_1=4.0 \text{ L}$$

$$T_1=288.15\text{K}$$

$$P_T= 0.87 \text{ atm}, P_{\text{H}_2\text{O}}=0.017 \text{ atm}, P_1= P_T -P_{\text{H}_2\text{O}} = 0.87 - 0.017 =0.853 \text{ atm}$$

$$V_2=??$$

$$P_2=1.01 \text{ atm} \quad T_2=400 \text{ K}$$

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

$$\frac{0.853 \times 4}{288.15} = \frac{1.01 \times V_2}{400}$$

$$V_2=4.69 \text{ L}$$

Ans: 4.69 L