

## Force and Motion-II



## Learning Outcomes

## By the end of the chapter student should be able:

- to identify friction force and its cause.
- to identify the static frictional force.
- calculate the value of static frictional force.
- to define the maximum static frictional force and how to calculate it.
- to identify kinetic friction force and how to calculate it.
- to define coefficients of static and kinetic friction.
- to apply Newton's laws including friction force to solve problems.
- to explain centripetal force in uniform circular motion and its direction.
- to calculate centripetal force.
- to identify the nature of centripetal force in different uniform circular motion.
- In this chapter we focus on the physics of: 1- Frictional force.
2- Centripetal force.


## 6-2 | Friction

A frictional force $\vec{f}$ is the force on a body when the body slides or attempts to slide along a surface. The force is always parallel to the surface and directed so as to oppose the sliding.


No motion, $\vec{f}_{s}$ : is the static friction


Acceleration, $\vec{f}_{k}$ : is the kinetic friction


Constant velocity

$$
\vec{F}=\vec{f}_{\mathrm{k}}
$$

## 6-3 | Properties of Friction

Frictional force

Static frictional
force:


Kinetic frictional force: $\vec{f}_{\mathrm{k}}$


## 6-3 | Properties of Friction

Property 1. If the body does not move, then the static frictional force $\vec{f}_{s}$ and the component of $\vec{F}$ that is parallel to the surface balance each other. They are equal in magnitude, and $\vec{f}_{s}$ is directed opposite that component of $\vec{F}$.


Property 2. The magnitude of $\vec{f}_{s}$ has a maximum value $f_{s, \text { max }}$ that is given by

$$
f_{s, \max }=\mu_{s} F_{N},
$$

where $\mu_{s}$ is the coefficient of static friction and $F_{N}$ is the magnitude of the normal force on the body from the surface.

Property 3. If the body begins to slide along the surface, the magnitude of the frictional force rapidly decreases to a value $f_{k}$ given by

$$
f_{k}=\mu_{k} F_{N}, \quad \text { where } \mu_{k} \text { is the coefficient of kinetic friction. }
$$



## Remember:

$\mu_{s}$ : Cofficient of static friction.
$\mu_{k}$ :Cofficient of kinetic friction.

- They are dimensionless.


## Sample Problem 6-1

If a car's wheels are "locked" (kept from rolling) durin emergency braking, the car slides along the roas Ripped-off bits of tire and small melted sections of roa form the "skid marks" that reveal that cold-weldin

(a) occurred during the slide. The record for the longest skid marks on a public road was reportedly set in 1960 by a Jaguar on the M1 highway in England (Fig. 6-3a) the marks were 290 m long! Assuming that $\mu_{k}=0.60$ and the car's acceleration was constant during the braking, how fast was the car going when the wheels became locked?

## Sample Problem 6-2

In Fig. 6-4a, a block of mass $m=3.0 \mathrm{~kg}$ slides along a floor while a force $\vec{F}$ of magnitude 12.0 N is applied to it

(a) at an upward angle $\theta$. The coefficient of kinetic friction between the block and the floor is $\mu_{k}=0.40$. What is the acceleration of the block?

## 6-5 I Uniform Circular Motion

A particle is in uniform circular motion if it travels around a circle or circular arc at constant speed.

## Centripetal acceleration

- magnitude $\quad a=\frac{v^{2}}{r}$
- direction: toward the center.

According to Newton's second law: The cause of the centripetal acceleration is a Force called the centripetal Force

- magnitude : $F=m a=m$
- direction: toward the center.



Friction Force is the centripetal force


Tension Force is the centripetal force


Gravity Force is the centripetal force

## Sample Problem 6-6

Igor is a cosmonaut on the International Space Station, in a circular orbit around Earth, at an altitude $h$ of 520 km and with a constant speed $v$ of $7.6 \mathrm{~km} / \mathrm{s}$. Igor's mass $m$ is 79 kg .
(a) What is his acceleration?
(b) What force does Earth exert on Igor?



#### Abstract

[1] WHAT IS PHYSICS? In this chapter we focus on the physics of three common types of force: frictional force, drag force, and centripetal force. An engineer preparing a car for the Indianapolis 500 must consider all three types. Frictional forces acting on the tires are crucial to the car's acceleration out of the pit and out of a curve (if the car hits an oil slick, the friction is lost and so is the car). Drag forces acting on the car from the passing air must be minimized or else the car will consume too much fuel and have to pit too early (even one 14 s pit stop can cost a driver the race). Centripetal forces are crucial in the turns (if there is insufficient centripetal force, the car slides into the wall). We start our discussion with frictional forces.


## 6-2 Friction

Frictional forces are unavoidable in our daily lives. If we were not able to counteract them, they would stop every moving object and bring to a halt every rotating shaft. About $20 \%$ of the gasoline used in an automobile is needed to counteract friction in the engine and in the drive train. On the other hand, if friction were totally absent, we could not get an automobile to go anywhere, and we could not walk or ride a bicycle. We could not hold a pencil, and, if we could, it would not write. Nails and screws would be useless, woven cloth would fall apart, and knots would untie.

Here we deal with the frictional forces that exist between dry solid surfaces, either stationary relative to each other or moving across each other at slow speeds. Consider three simple thought experiments:

1. Send a book sliding across a long horizontal counter. As expected, the book slows and then stops. This means the book must have an acceleration parallel to the counter surface, in the direction opposite the book's velocity. From Newton's second law, then, a force must act on the book parallel to the counter surface, in the direction opposite its velocity. That force is a frictional force.
2. Push horizontally on the book to make it travel at constant velocity along the counter. Can the force from you be the only horizontal force on the book? No, because then the book would accelerate. From Newton's second law, there must be a second force, directed opposite your force but with the same magnitude, so that the two forces balance. That second force is a frictional force, directed parallel to the counter.
3. Push horizontally on a heavy crate. The crate does not move. From Newton's second law, a second force must also be acting on the crate to counteract your force. Moreover, this second force must be directed opposite your force and have the same magnitude as your force, so that the two forces balance. That second force is a frictional force. Push even harder. The crate still does not move. Apparently the frictional force can change in magnitude so that the two
forces still balance. Now push with all your strength. The crate begins to slide. Evidently, there is a maximum magnitude of the frictional force. When you exceed that maximum magnitude, the crate slides.

Figure 6-1 shows a similar situation. In Fig. 6-1a, a block rests on a tabletop, with the gravitational force $\vec{F}_{g}$ balanced by a normal force $\vec{F}_{N}$. In Fig. 6-1b, you exert a force $\vec{F}$ on the block, attempting to pull it to the left. In response, a

Fig. 6-1 (a) The forces on a stationary block. $(b-d)$ An external force $\vec{F}$, applied to the block, is balanced by a static frictional force $\vec{f}_{s}$. As $F$ is increased, $f_{s}$ also increases, until $f_{s}$ reaches a certain maximum value. (e) The block then "breaks away," accelerating suddenly in the direction of $\vec{F} .(f)$ If the block is now to move with constant velocity, $F$ must be reduced from the maximum value it had just before the block broke away. $(g)$ Some experimental results for the sequence ( $a$ ) through ( $f$ ).

There is no attempt at sliding. Thus, no friction and no motion.

## Force $\vec{F}$ attempts

 sliding but is balanced by the frictional force. No motion.Force $\vec{F}$ is now stronger but is still balanced by the frictional force. No motion.

Force $\vec{F}$ is now even stronger but is still balanced by the frictional force. No motion.

Finally, the applied force has overwhelmed the static frictional force. Block slides and accelerates.

To maintain the speed, weaken force $\vec{F}$ to match the weak frictional force. can only match growing applied force.

(b)


Frictional force $=F$
(c)

(d)

(e)


Same weak kinetic frictional force

frictional force $\vec{f}_{s}$ is directed to the right, exactly balancing your force. The force $\vec{f}_{s}$ is called the static frictional force. The block does not move.

Figures 6-1c and 6-1d show that as you increase the magnitude of your applied force, the magnitude of the static frictional force $\vec{f}_{s}$ also increases and the block remains at rest. When the applied force reaches a certain magnitude, however, the block "breaks away" from its intimate contact with the tabletop and accelerates leftward (Fig. 6-1e). The frictional force that then opposes the motion is called the kinetic frictional force $\vec{f}_{k}$.

Usually, the magnitude of the kinetic frictional force, which acts when there is motion, is less than the maximum magnitude of the static frictional force, which acts when there is no motion. Thus, if you wish the block to move across the surface with a constant speed, you must usually decrease the magnitude of the applied force once the block begins to move, as in Fig. 6-1f. As an example, Fig. 6-1 $g$ shows the results of an experiment in which the force on a block was slowly increased until breakaway occurred. Note the reduced force needed to keep the block moving at constant speed after breakaway.

A frictional force is, in essence, the vector sum of many forces acting between the surface atoms of one body and those of another body. If two highly polished and carefully cleaned metal surfaces are brought together in a very good vacuum (to keep them clean), they cannot be made to slide over each other. Because the surfaces are so smooth, many atoms of one surface contact many atoms of the other surface, and the surfaces cold-weld together instantly, forming a single piece of metal. If a machinist's specially polished gage blocks are brought together in air, there is less atom-to-atom contact, but the blocks stick firmly to each other and can be separated only by means of a wrenching motion. Usually, however, this much atom-to-atom contact is not possible. Even a highly polished metal surface is far from being flat on the atomic scale. Moreover, the surfaces of everyday objects have layers of oxides and other contaminants that reduce cold-welding.

When two ordinary surfaces are placed together, only the high points touch each other. (It is like having the Alps of Switzerland turned over and placed down on the Alps of Austria.) The actual microscopic area of contact is much less than the apparent macroscopic contact area, perhaps by a factor of $10^{4}$. Nonetheless, many contact points do cold-weld together. These welds produce static friction when an applied force attempts to slide the surfaces relative to each other.

If the applied force is great enough to pull one surface across the other, there is first a tearing of welds (at breakaway) and then a continuous re-forming and tearing of welds as movement occurs and chance contacts are made (Fig. 6-2). The kinetic frictional force $\vec{f}_{k}$ that opposes the motion is the vector sum of the forces at those many chance contacts.

If the two surfaces are pressed together harder, many more points coldweld. Now getting the surfaces to slide relative to each other requires a greater applied force: The static frictional force $\vec{f}_{s}$ has a greater maximum value. Once

Fig. 6-2 The mechanism of sliding friction. (a) The upper surface is sliding to the right over the lower surface in this enlarged view. (b) A detail, showing two spots where cold-welding has occurred. Force is required to break the welds and maintain the motion.

(a)

(b)
the surfaces are sliding, there are many more points of momentary cold-welding, so the kinetic frictional force $\vec{f}_{k}$ also has a greater magnitude.

Often, the sliding motion of one surface over another is "jerky" because the two surfaces alternately stick together and then slip. Such repetitive stick-andslip can produce squeaking or squealing, as when tires skid on dry pavement, fingernails scratch along a chalkboard, or a rusty hinge is opened. It can also produce beautiful and captivating sounds, as in music when a bow is drawn properly across a violin string.

## 6-3 Properties of Friction

Experiment shows that when a dry and unlubricated body presses against a surface in the same condition and a force $\vec{F}$ attempts to slide the body along the surface, the resulting frictional force has three properties:
Property 1. If the body does not move, then the static frictional force $\vec{f}_{s}$ and the component of $\vec{F}$ that is parallel to the surface balance each other. They are equal in magnitude, and $\vec{f}_{s}$ is directed opposite that component of $\vec{F}$.
Property 2. The magnitude of $\vec{f}_{s}$ has a maximum value $f_{s, \text { max }}$ that is given by

$$
\begin{equation*}
f_{s, \max }=\mu_{s} F_{N} \tag{6-1}
\end{equation*}
$$

where $\mu_{s}$ is the coefficient of static friction and $F_{N}$ is the magnitude of the normal force on the body from the surface. If the magnitude of the component of $\vec{F}$ that is parallel to the surface exceeds $f_{s, \text { max }}$, then the body begins to slide along the surface.
Property 3. If the body begins to slide along the surface, the magnitude of the frictional force rapidly decreases to a value $f_{k}$ given by

$$
\begin{equation*}
f_{k}=\mu_{k} F_{N} \tag{6-2}
\end{equation*}
$$

where $\mu_{k}$ is the coefficient of kinetic friction. Thereafter, during the sliding, a kinetic frictional force $\vec{f}_{k}$ with magnitude given by Eq. 6-2 opposes the motion.
The magnitude $F_{N}$ of the normal force appears in properties 2 and 3 as a measure of how firmly the body presses against the surface. If the body presses harder, then, by Newton's third law, $F_{N}$ is greater. Properties 1 and 2 are worded in terms of a single applied force $\vec{F}$, but they also hold for the net force of several applied forces acting on the body. Equations 6-1 and 6-2 are not vector equations; the direction of $\vec{f}_{s}$ or $\vec{f}_{k}$ is always parallel to the surface and opposed to the attempted sliding, and the normal force $\vec{F}_{N}$ is perpendicular to the surface.

The coefficients $\mu_{s}$ and $\mu_{k}$ are dimensionless and must be determined experimentally. Their values depend on certain properties of both the body and the surface; hence, they are usually referred to with the preposition "between," as in "the value of $\mu_{s}$ between an egg and a Teflon-coated skillet is 0.04 , but that between rock-climbing shoes and rock is as much as 1.2 ." We assume that the value of $\mu_{k}$ does not depend on the speed at which the body slides along the surface.

## CHECKPOINT 1

A block lies on a floor. (a) What is the magnitude of the frictional force on it from the floor? (b) If a horizontal force of 5 N is now applied to the block, but the block does not move, what is the magnitude of the frictional force on it? (c) If the maximum value $f_{s, \text { max }}$ of the static frictional force on the block is 10 N , will the block move if the magnitude of the horizontally applied force is 8 N ? (d) If it is 12 N ? (e) What is the magnitude of the frictional force in part (c)?

## Kinetic friction, constant acceleration, locked wheels

If a car's wheels are "locked" (kept from rolling) during emergency braking, the car slides along the road. Ripped-off bits of tire and small melted sections of road form the "skid marks" that reveal that cold-welding occurred during the slide. The record for the longest skid marks on a public road was reportedly set in 1960 by a Jaguar on the M1 highway in England (Fig. 6-3a) - the marks were 290 m long! Assuming that $\mu_{k}=0.60$ and the car's acceleration was constant during the braking, how fast was the car going when the wheels became locked?

## KEY IDEAS

(1) Because the acceleration $a$ is assumed constant, we can use the constant-acceleration equations of Table 2-1 to find the car's initial speed $v_{0}$. (2) If we neglect the effects of the air on the car, acceleration $a$ was due only to a kinetic frictional force $\vec{f}_{k}$ on the car from the road, directed opposite the direction of the car's motion, assumed to be in the positive direction of an $x$ axis (Fig. 6-3b). We can relate this force to the acceleration by writing Newton's second law for $x$ components ( $F_{\text {net }, x}=m a_{x}$ ) as

$$
\begin{equation*}
-f_{k}=m a \tag{6-3}
\end{equation*}
$$

where $m$ is the car's mass. The minus sign indicates the direction of the kinetic frictional force.

Calculations: From Eq. 6-2, the frictional force has the magnitude $f_{k}=\mu_{k} F_{N}$, where $F_{N}$ is the magnitude of the normal force on the car from the road. Because the car is not accelerating vertically, we know from Fig. $6-3 b$ and Newton's second law that the magnitude of $\vec{F}_{N}$ is equal to the magnitude of the gravitational force $\vec{F}_{g}$ on the car, which is $m g$. Thus, $F_{N}=m g$.

Now solving Eq. 6-3 for $a$ and substituting $f_{k}=\mu_{k} F_{N}=$ $\mu_{k} m g$ for $f_{k}$ yield

$$
\begin{equation*}
a=-\frac{f_{k}}{m}=-\frac{\mu_{k} m g}{m}=-\mu_{k} g \tag{6-4}
\end{equation*}
$$


(a)

(b)

Fig. 6-3 (a) A car sliding to the right and finally stopping after a displacement of 290 m . (b) A free-body diagram for the car.
where the minus sign indicates that the acceleration is in the negative direction of the $x$ axis, opposite the direction of the velocity. Next, let's use Eq. 2-16,

$$
\begin{equation*}
v^{2}=v_{0}^{2}+2 a\left(x-x_{0}\right) \tag{6-5}
\end{equation*}
$$

from the constant-acceleration equations of Chapter 2. We know that the displacement $x-x_{0}$ was 290 m and assume that the final speed $v$ was 0 . Substituting for $a$ from Eq. 6-4 and solving for $v_{0}$ give

$$
\begin{align*}
v_{0} & =\sqrt{2 \mu_{k} g\left(x-x_{0}\right)}  \tag{6-6}\\
& =\sqrt{(2)(0.60)\left(9.8 \mathrm{~m} / \mathrm{s}^{2}\right)(290 \mathrm{~m})} \\
& =58 \mathrm{~m} / \mathrm{s}=210 \mathrm{~km} / \mathrm{h}
\end{align*}
$$

(Answer)
We assumed that $v=0$ at the far end of the skid marks. Actually, the marks ended only because the Jaguar left the road after 290 m . So $v_{0}$ was at least $210 \mathrm{~km} / \mathrm{h}$.

## Sample Problem

## Friction, applied force at an angle

In Fig. 6-4 $a$, a block of mass $m=3.0 \mathrm{~kg}$ slides along a floor while a force $\vec{F}$ of magnitude 12.0 N is applied to it at an upward angle $\theta$. The coefficient of kinetic friction between the block and the floor is $\mu_{k}=0.40$. We can vary $\theta$ from 0 to $90^{\circ}$ (the block remains on the floor). What $\theta$ gives the maximum value of the block's acceleration magnitude $a$ ?

## KEY IDEAS

Because the block is moving, a kinetic frictional force acts on it. The magnitude is given by Eq. 6-2 $\left(f_{k}=\mu_{k} F_{N}\right.$, where $F_{N}$ is the normal force). The direction is opposite the motion (the friction opposes the sliding).

Calculating $\boldsymbol{F}_{N}$ : Because we need the magnitude $f_{k}$ of the frictional force, we first must calculate the magnitude $F_{N}$ of the normal force. Figure $6-4 b$ is a free-body diagram showing the forces along the vertical $y$ axis. The normal force is upward, the gravitational force $\vec{F}_{g}$ with magnitude $m g$ is downward, and (note) the vertical component $F_{y}$ of the applied force is upward. That component is shown in Fig. 6-4c, where we can see that $F_{y}=F \sin \theta$. We can write Newton's second law $\left(\vec{F}_{\text {net }}=m \vec{a}\right)$ for those forces along the $y$ axis as

$$
\begin{equation*}
F_{N}+F \sin \theta-m g=m(0), \tag{6-7}
\end{equation*}
$$

where we substituted zero for the acceleration along the $y$ axis (the block does not even move along that axis). Thus,

$$
\begin{equation*}
F_{N}=m g-F \sin \theta . \tag{6-8}
\end{equation*}
$$

Calculating acceleration a: Figure 6-4d is a free-body diagram for motion along the $x$ axis. The horizontal component $F_{x}$ of the applied force is rightward; from Fig. 6-4c, we see that $F_{x}=F \cos \theta$. The frictional force has magnitude $f_{k}$ ( $=\mu_{k} F_{N}$ ) and is leftward. Writing Newton's second law for motion along the $x$ axis gives us

$$
\begin{equation*}
F \cos \theta-\mu_{k} F_{N}=m a \tag{6-9}
\end{equation*}
$$

Substituting for $F_{N}$ from Eq. 6-8 and solving for $a$ lead to

$$
\begin{equation*}
a=\frac{F}{m} \cos \theta-\mu_{k}\left(g-\frac{F}{m} \sin \theta\right) . \tag{6-10}
\end{equation*}
$$

Finding a maximum: To find the value of $\theta$ that maximizes $a$, we take the derivative of $a$ with respect to $\theta$ and set the result equal to zero:

$$
\begin{equation*}
\frac{d a}{d \theta}=-\frac{F}{m} \sin \theta+\mu_{k} \frac{F}{m} \cos \theta=0 \tag{6-11}
\end{equation*}
$$

Rearranging and using the identity $(\sin \theta) /(\cos \theta)=\tan \theta$ give us

$$
\begin{equation*}
\tan \theta=\mu_{k} \tag{6-12}
\end{equation*}
$$

Solving for $\theta$ and substituting the given $\mu_{k}=0.40$, we find that the acceleration will be maximum if

$$
\begin{align*}
\theta & =\tan ^{-1} \mu_{k}  \tag{6-13}\\
& =21.8^{\circ} \approx 22^{\circ} .
\end{align*}
$$

(Answer)
Comment: As we increase $\theta$ from 0 , the acceleration tends to change in two opposing ways. First, more of the applied force $\vec{F}$ is upward, relieving the normal force. The decrease in the normal force causes a decrease in the frictional force, which opposes the block's motion. Thus, with the increase in $\theta$, the block's acceleration tends to increase. However, second, the increase in $\theta$ also decreases the horizontal component of $\vec{F}$, and so the block's acceleration tends to decrease. These opposing tendencies produce a maximum acceleration at $\theta=22^{\circ}$.

Fig. 6-4 (a) A force is applied to a moving block. (b) The vertical forces. (c) The components of the applied force. $(d)$ The horizontal forces and acceleration.


Additional examples, video, and practice available at WileyPLUS

## 6-4 The Drag Force and Terminal Speed

A fluid is anything that can flow-generally either a gas or a liquid. When there is a relative velocity between a fluid and a body (either because the body moves through the fluid or because the fluid moves past the body), the body experiences a drag force $\vec{D}$ that opposes the relative motion and points in the direction in which the fluid flows relative to the body.

Here we examine only cases in which air is the fluid, the body is blunt (like a baseball) rather than slender (like a javelin), and the relative motion is fast enough so that the air becomes turbulent (breaks up into swirls) behind the body.


Fig. 6-5 This skier crouches in an "egg position" so as to minimize her effective cross-sectional area and thus minimize the air drag acting on her. (Karl-Josef Hildenbrand/dpa/Landov LLC)


Fig. 6-6 The forces that act on a body falling through air: (a) the body when it has just begun to fall and $(b)$ the free-body diagram a little later, after a drag force has developed. (c) The drag force has increased until it balances the gravitational force on the body. The body now falls at its constant terminal speed.

|  | Table 6-1 |  |
| :--- | :---: | :---: |
| Some Terminal Speeds in Air |  |  |
| Object | Terminal Speed (m/s) | $95 \%$ Distance $^{a}(\mathrm{~m})$ |
| Shot (from shot put) | 145 | 2500 |
| Sky diver (typical) | 60 | 430 |
| Baseball | 42 | 210 |
| Tennis ball | 31 | 115 |
| Basketball | 20 | 47 |
| Ping-Pong ball | 9 | 10 |
| Raindrop (radius $=1.5 \mathrm{~mm})$ | 7 | 6 |
| Parachutist (typical) | 5 | 3 |

${ }^{a}$ This is the distance through which the body must fall from rest to reach $95 \%$ of its terminal speed. Source: Adapted from Peter J. Brancazio, Sport Science, 1984, Simon \& Schuster, New York.

In such cases, the magnitude of the drag force $\vec{D}$ is related to the relative speed $v$ by an experimentally determined drag coefficient $C$ according to

$$
\begin{equation*}
D=\frac{1}{2} C \rho A v^{2} \tag{6-14}
\end{equation*}
$$

where $\rho$ is the air density (mass per volume) and $A$ is the effective cross-sectional area of the body (the area of a cross section taken perpendicular to the velocity $\vec{v}$ ). The drag coefficient $C$ (typical values range from 0.4 to 1.0 ) is not truly a constant for a given body because if $v$ varies significantly, the value of $C$ can vary as well. Here, we ignore such complications.

Downhill speed skiers know well that drag depends on $A$ and $v^{2}$. To reach high speeds a skier must reduce $D$ as much as possible by, for example, riding the skis in the "egg position" (Fig. 6-5) to minimize $A$.

When a blunt body falls from rest through air, the drag force $\vec{D}$ is directed upward; its magnitude gradually increases from zero as the speed of the body increases. This upward force $\vec{D}$ opposes the downward gravitational force $\vec{F}_{g}$ on the body. We can relate these forces to the body's acceleration by writing Newton's second law for a vertical $y$ axis $\left(F_{\text {net }, y}=m a_{y}\right)$ as

$$
\begin{equation*}
D-F_{g}=m a \tag{6-15}
\end{equation*}
$$

where $m$ is the mass of the body. As suggested in Fig. 6-6, if the body falls long enough, $D$ eventually equals $F_{g}$. From Eq. 6-15, this means that $a=0$, and so the body's speed no longer increases. The body then falls at a constant speed, called the terminal speed $v_{t}$.

To find $v_{t}$, we set $a=0$ in Eq. 6-15 and substitute for $D$ from Eq. 6-14, obtaining

$$
\frac{1}{2} C \rho A v_{t}^{2}-F_{g}=0
$$

which gives $\quad v_{t}=\sqrt{\frac{2 F_{g}}{C \rho A}}$.

Table 6-1 gives values of $v_{t}$ for some common objects.
According to calculations* based on Eq. 6-14, a cat must fall about six floors to reach terminal speed. Until it does so, $F_{g}>D$ and the cat accelerates downward because of the net downward force. Recall from Chapter 2 that your body is an accelerometer, not a speedometer. Because the cat also senses the acceleration, it is frightened and keeps its feet underneath its body, its head tucked in, and its spine bent upward, making $A$ small, $v_{t}$ large, and injury likely.
*W. O. Whitney and C. J. Mehlhaff,"High-Rise Syndrome in Cats." The Journal of the American Veterinary Medical Association, 1987.

However, if the cat does reach $v_{t}$ during a longer fall, the acceleration vanishes and the cat relaxes somewhat, stretching its legs and neck horizontally outward and straightening its spine (it then resembles a flying squirrel). These actions increase area $A$ and thus also, by Eq. 6-14, the drag $D$. The cat begins to slow because now $D>F_{g}$ (the net force is upward), until a new, smaller $v_{t}$ is reached. The decrease in $v_{t}$ reduces the possibility of serious injury on landing. Just before the end of the fall, when it sees it is nearing the ground, the cat pulls its legs back beneath its body to prepare for the landing.

Humans often fall from great heights for the fun of skydiving. However, in April 1987, during a jump, sky diver Gregory Robertson noticed that fellow sky diver Debbie Williams had been knocked unconscious in a collision with a third sky diver and was unable to open her parachute. Robertson, who was well above Williams at the time and who had not yet opened his parachute for the 4 km plunge, reoriented his body head-down so as to minimize $A$ and maximize his downward speed. Reaching an estimated $v_{t}$ of $320 \mathrm{~km} / \mathrm{h}$, he caught up with Williams and then went into a horizontal "spread eagle" (as in Fig. 6-7) to increase $D$ so that he could grab her. He opened her parachute and then, after releasing her, his own, a scant 10 s before impact. Williams received extensive internal injuries due to her lack of control on landing but survived.


Fig. 6-7 Sky divers in a horizontal "spread eagle" maximize air drag. (Steve Fitchett/Taxi/Getty Images)

## Sample Problem

## Terminal speed of falling raindrop

A raindrop with radius $R=1.5 \mathrm{~mm}$ falls from a cloud that is at height $h=1200 \mathrm{~m}$ above the ground. The drag coefficient $C$ for the drop is 0.60 . Assume that the drop is spherical throughout its fall. The density of water $\rho_{w}$ is $1000 \mathrm{~kg} / \mathrm{m}^{3}$, and the density of air $\rho_{a}$ is $1.2 \mathrm{~kg} / \mathrm{m}^{3}$.
(a) As Table 6-1 indicates, the raindrop reaches terminal speed after falling just a few meters. What is the terminal speed?

## KEY IDEA

The drop reaches a terminal speed $v_{t}$ when the gravitational force on it is balanced by the air drag force on it, so its acceleration is zero. We could then apply Newton's second law and the drag force equation to find $v_{t}$, but Eq. 6-16 does all that for us.

Calculations: To use Eq. 6-16, we need the drop's effective cross-sectional area $A$ and the magnitude $F_{g}$ of the gravitational force. Because the drop is spherical, $A$ is the area of a circle $\left(\pi R^{2}\right)$ that has the same radius as the sphere. To find $F_{g}$, we use three facts: (1) $F_{g}=m g$, where $m$ is the drop's mass; (2) the (spherical) drop's volume is $V=\frac{4}{3} \pi R^{3}$; and (3) the density of the water in the drop is the mass per volume, or $\rho_{w}=m / V$. Thus, we find

$$
F_{g}=V \rho_{w} g=\frac{4}{3} \pi R^{3} \rho_{w} g
$$

We next substitute this, the expression for $A$, and the given data into Eq. 6-16. Being careful to distinguish between the air den-
sity $\rho_{a}$ and the water density $\rho_{w}$, we obtain

$$
\begin{aligned}
v_{t} & =\sqrt{\frac{2 F_{g}}{C \rho_{a} A}}=\sqrt{\frac{8 \pi R^{3} \rho_{w} g}{3 C \rho_{a} \pi R^{2}}}=\sqrt{\frac{8 R \rho_{w} g}{3 C \rho_{a}}} \\
& =\sqrt{\frac{(8)\left(1.5 \times 10^{-3} \mathrm{~m}\right)\left(1000 \mathrm{~kg} / \mathrm{m}^{3}\right)\left(9.8 \mathrm{~m} / \mathrm{s}^{2}\right)}{(3)(0.60)\left(1.2 \mathrm{~kg} / \mathrm{m}^{3}\right)}} \\
& =7.4 \mathrm{~m} / \mathrm{s} \approx 27 \mathrm{~km} / \mathrm{h} .
\end{aligned}
$$

(Answer)
Note that the height of the cloud does not enter into the calculation.
(b) What would be the drop's speed just before impact if there were no drag force?

## KEY IDEA

With no drag force to reduce the drop's speed during the fall, the drop would fall with the constant free-fall acceleration $g$, so the constant-acceleration equations of Table 2-1 apply.
Calculation: Because we know the acceleration is $g$, the initial velocity $v_{0}$ is 0 , and the displacement $x-x_{0}$ is $-h$, we use Eq. 2-16 to find $v$ :

$$
\begin{aligned}
v & =\sqrt{2 g h}=\sqrt{(2)\left(9.8 \mathrm{~m} / \mathrm{s}^{2}\right)(1200 \mathrm{~m})} \\
& =153 \mathrm{~m} / \mathrm{s} \approx 550 \mathrm{~km} / \mathrm{h}
\end{aligned}
$$

(Answer)
Had he known this, Shakespeare would scarcely have written, "it droppeth as the gentle rain from heaven, upon the place beneath." In fact, the speed is close to that of a bullet from a large-caliber handgun!

## 6-5 Uniform Circular Motion

From Section 4-7, recall that when a body moves in a circle (or a circular arc) at constant speed $v$, it is said to be in uniform circular motion. Also recall that the body has a centripetal acceleration (directed toward the center of the circle) of constant magnitude given by

$$
\begin{equation*}
a=\frac{v^{2}}{R} \quad \text { (centripetal acceleration) } \tag{6-17}
\end{equation*}
$$

where $R$ is the radius of the circle.
Let us examine two examples of uniform circular motion:

1. Rounding a curve in a car. You are sitting in the center of the rear seat of a car moving at a constant high speed along a flat road. When the driver suddenly turns left, rounding a corner in a circular arc, you slide across the seat toward the right and then jam against the car wall for the rest of the turn. What is going on?

While the car moves in the circular arc, it is in uniform circular motion; that is, it has an acceleration that is directed toward the center of the circle. By Newton's second law, a force must cause this acceleration. Moreover, the force must also be directed toward the center of the circle. Thus, it is a centripetal force, where the adjective indicates the direction. In this example, the centripetal force is a frictional force on the tires from the road; it makes the turn possible.

If you are to move in uniform circular motion along with the car, there must also be a centripetal force on you. However, apparently the frictional force on you from the seat was not great enough to make you go in a circle with the car. Thus, the seat slid beneath you, until the right wall of the car jammed into you. Then its push on you provided the needed centripetal force on you, and you joined the car's uniform circular motion.
2. Orbiting Earth. This time you are a passenger in the space shuttle Atlantis. As it and you orbit Earth, you float through your cabin. What is going on?

Both you and the shuttle are in uniform circular motion and have accelerations directed toward the center of the circle. Again by Newton's second law, centripetal forces must cause these accelerations. This time the centripetal forces are gravitational pulls (the pull on you and the pull on the shuttle) exerted by Earth and directed radially inward, toward the center of Earth.
In both car and shuttle you are in uniform circular motion, acted on by a centripetal force - yet your sensations in the two situations are quite different. In the car, jammed up against the wall, you are aware of being compressed by the wall. In the orbiting shuttle, however, you are floating around with no sensation of any force acting on you. Why this difference?

The difference is due to the nature of the two centripetal forces. In the car, the centripetal force is the push on the part of your body touching the car wall. You can sense the compression on that part of your body. In the shuttle, the centripetal force is Earth's gravitational pull on every atom of your body. Thus, there is no compression (or pull) on any one part of your body and no sensation of a force acting on you. (The sensation is said to be one of "weightlessness," but that description is tricky. The pull on you by Earth has certainly not disappeared and, in fact, is only a little less than it would be with you on the ground.)

Another example of a centripetal force is shown in Fig. 6-8. There a hockey puck moves around in a circle at constant speed $v$ while tied to a string looped around a central peg. This time the centripetal force is the radially inward pull on the puck from the string. Without that force, the puck would slide off in a straight line instead of moving in a circle.


The puck moves in uniform circular motion only because of a toward-thecenter force.

Fig. 6-8 An overhead view of a hockey puck moving with constant speed $v$ in a circular path of radius $R$ on a horizontal frictionless surface. The centripetal force on the puck is $\vec{T}$, the pull from the string, directed inward along the radial axis $r$ extending through the puck.

Note again that a centripetal force is not a new kind of force. The name merely indicates the direction of the force. It can, in fact, be a frictional force, a gravitational force, the force from a car wall or a string, or any other force. For any situation:

A centripetal force accelerates a body by changing the direction of the body's velocity without changing the body's speed.

From Newton's second law and Eq. 6-17 $\left(a=v^{2} / R\right)$, we can write the magnitude $F$ of a centripetal force (or a net centripetal force) as

$$
\begin{equation*}
F=m \frac{v^{2}}{R} \quad \text { (magnitude of centripetal force). } \tag{6-18}
\end{equation*}
$$

Because the speed $v$ here is constant, the magnitudes of the acceleration and the force are also constant.

However, the directions of the centripetal acceleration and force are not constant; they vary continuously so as to always point toward the center of the circle. For this reason, the force and acceleration vectors are sometimes drawn along a radial axis $r$ that moves with the body and always extends from the center of the circle to the body, as in Fig. 6-8. The positive direction of the axis is radially outward, but the acceleration and force vectors point radially inward.

## CHECKPOINT 2

When you ride in a Ferris wheel at constant speed, what are the directions of your acceleration $\vec{a}$ and the normal force $\vec{F}_{N}$ on you (from the always upright seat) as you pass through (a) the highest point and (b) the lowest point of the ride?

## Sample Problem

## Vertical circular loop, Diavolo

In a 1901 circus performance, Allo "Dare Devil" Diavolo introduced the stunt of riding a bicycle in a loop-the-loop (Fig. 6-9a). Assuming that the loop is a circle with radius $R=2.7 \mathrm{~m}$, what is the least speed $v$ that Diavolo and his bicycle could have at the top of the loop to remain in contact with it there?

## KEY IDEA

We can assume that Diavolo and his bicycle travel through the top of the loop as a single particle in uniform circular motion. Thus, at the top, the acceleration $\vec{a}$ of this particle must have the magnitude $a=v^{2} / R$ given by Eq. 6-17 and be directed downward, toward the center of the circular loop.

(a)

(b)

Fig. 6-9 (a) Contemporary advertisement for Diavolo and (b) free-body diagram for the performer at the top of the loop. (Photograph in part a reproduced with permission of Circus World Museum)

Calculations: The forces on the particle when it is at the top of the loop are shown in the free-body diagram of Fig 6$9 b$. The gravitational force $\vec{F}_{g}$ is downward along a $y$ axis; so is the normal force $\vec{F}_{N}$ on the particle from the loop; so also is the centripetal acceleration of the particle. Thus, Newton's second law for $y$ components ( $F_{\text {net }, y}=m a_{y}$ ) gives us
and

$$
\begin{align*}
-F_{N}-F_{g} & =m(-a) \\
-F_{N}-m g & =m\left(-\frac{v^{2}}{R}\right) \tag{6-19}
\end{align*}
$$

If the particle has the least speed $v$ needed to remain in contact, then it is on the verge of losing contact with the loop (falling away from the loop), which means that $F_{N}=0$ at the top of the loop (the particle and loop touch but without any normal force). Substituting 0 for $F_{N}$ in Eq. 6-19, solving for $v$, and then substituting known values give us

$$
\begin{aligned}
v & =\sqrt{g R}=\sqrt{\left(9.8 \mathrm{~m} / \mathrm{s}^{2}\right)(2.7 \mathrm{~m})} \\
& =5.1 \mathrm{~m} / \mathrm{s} .
\end{aligned}
$$

(Answer)
Comments: Diavolo made certain that his speed at the top of the loop was greater than $5.1 \mathrm{~m} / \mathrm{s}$ so that he did not lose contact with the loop and fall away from it. Note that this speed requirement is independent of the mass of Diavolo and his bicycle. Had he feasted on, say, pierogies before his performance, he still would have had to exceed only $5.1 \mathrm{~m} / \mathrm{s}$ to maintain contact as he passed through the top of the loop.

## Sample Problem

## Car in flat circular turn

Upside-down racing: A modern race car is designed so that the passing air pushes down on it, allowing the car to travel much faster through a flat turn in a Grand Prix without friction failing. This downward push is called negative lift. Can a race car have so much negative lift that it could be driven upside down on a long ceiling, as done fictionally by a sedan in the first Men in Black movie?

Figure 6-10a represents a Grand Prix race car of mass $m=600 \mathrm{~kg}$ as it travels on a flat track in a circular arc of radius $R=100 \mathrm{~m}$. Because of the shape of the car and the wings on it, the passing air exerts a negative lift $\vec{F}_{L}$ downward on the car. The coefficient of static friction between the tires and the track is 0.75 . (Assume that the forces on the four tires are identical.)
(a) If the car is on the verge of sliding out of the turn when its speed is $28.6 \mathrm{~m} / \mathrm{s}$, what is the magnitude of the negative lift $\vec{F}_{L}$ acting downward on the car?

KEY IDEAS

1. A centripetal force must act on the car because the car is moving around a circular arc; that force must be directed toward the center of curvature of the arc (here, that is horizontally).
2. The only horizontal force acting on the car is a frictional force on the tires from the road. So the required centripetal force is a frictional force.
3. Because the car is not sliding, the frictional force must be a static frictional force $\vec{f}_{s}$ (Fig. 6-10a).
4. Because the car is on the verge of sliding, the magnitude $f_{s}$ is equal to the maximum value $f_{s, \text { max }}=\mu_{s} F_{N}$, where $F_{N}$ is the magnitude of the normal force $\vec{F}_{N}$ acting on the car from the track.

Radial calculations: The frictional force $\vec{f}_{s}$ is shown in the free-body diagram of Fig. 6-10b. It is in the negative direc-
tion of a radial axis $r$ that always extends from the center of curvature through the car as the car moves. The force produces a centripetal acceleration of magnitude $v^{2} / R$. We can relate the force and acceleration by writing Newton's second law for components along the $r$ axis $\left(F_{\text {net }, r}=m a_{r}\right)$ as

$$
\begin{equation*}
-f_{s}=m\left(-\frac{v^{2}}{R}\right) . \tag{6-20}
\end{equation*}
$$

Substituting $f_{s, \text { max }}=\mu_{s} F_{N}$ for $f_{s}$ leads us to

$$
\begin{equation*}
\mu_{s} F_{N}=m\left(\frac{v^{2}}{R}\right) . \tag{6-21}
\end{equation*}
$$

Vertical calculations: Next, let's consider the vertical forces on the car. The normal force $\vec{F}_{N}$ is directed up, in the positive direction of the $y$ axis in Fig. 6-10b. The gravitational force $\vec{F}_{g}=m \vec{g}$ and the negative lift $\vec{F}_{L}$ are directed down. The acceleration of the car along the $y$ axis is zero. Thus we can write Newton's second law for components along the $y$ axis $\left(F_{\text {net }, y}=m a_{y}\right)$ as

$$
F_{N}-m g-F_{L}=0,
$$

or

$$
\begin{equation*}
F_{N}=m g+F_{L} . \tag{6-22}
\end{equation*}
$$

Combining results: Now we can combine our results along the two axes by substituting Eq. 6-22 for $F_{N}$ in Eq. 6-21. Doing so and then solving for $F_{L}$ lead to

$$
\begin{aligned}
F_{L} & =m\left(\frac{v^{2}}{\mu_{s} R}-g\right) \\
& =(600 \mathrm{~kg})\left(\frac{(28.6 \mathrm{~m} / \mathrm{s})^{2}}{(0.75)(100 \mathrm{~m})}-9.8 \mathrm{~m} / \mathrm{s}^{2}\right) \\
& =663.7 \mathrm{~N} \approx 660 \mathrm{~N} .
\end{aligned}
$$

(Answer)
(b) The magnitude $F_{L}$ of the negative lift on a car depends on the square of the car's speed $v^{2}$, just as the drag force does (Eq. 6-14). Thus, the negative lift on the car here is greater when the car travels faster, as it does on a straight section of track. What is the magnitude of the negative lift for a speed of $90 \mathrm{~m} / \mathrm{s}$ ?

## KEY IDEA

$F_{L}$ is proportional to $v^{2}$.
Calculations: Thus we can write a ratio of the negative lift $F_{L, 90}$ at $v=90 \mathrm{~m} / \mathrm{s}$ to our result for the negative lift $F_{L}$ at $v=$ $28.6 \mathrm{~m} / \mathrm{s}$ as

$$
\frac{F_{L, 90}}{F_{L}}=\frac{(90 \mathrm{~m} / \mathrm{s})^{2}}{(28.6 \mathrm{~m} / \mathrm{s})^{2}}
$$

Substituting our known negative lift of $F_{L}=663.7 \mathrm{~N}$ and solving for $F_{L, 90}$ give us

$$
F_{L, 90}=6572 \mathrm{~N} \approx 6600 \mathrm{~N} .
$$

(Answer)
Upside-down racing: The gravitational force is, of course, the force to beat if there is a chance of racing upside down:

$$
\begin{aligned}
F_{g} & =m g=(600 \mathrm{~kg})\left(9.8 \mathrm{~m} / \mathrm{s}^{2}\right) \\
& =5880 \mathrm{~N} .
\end{aligned}
$$

With the car upside down, the negative lift is an upward force of 6600 N , which exceeds the downward 5880 N . Thus, the car could run on a long ceiling provided that it moves at about $90 \mathrm{~m} / \mathrm{s}(=324 \mathrm{~km} / \mathrm{h}=201 \mathrm{mi} / \mathrm{h})$. However, moving that fast while right side up on a horizontal track is dangerous enough, so you are not likely to see upside-down racing except in the movies.


Fig. 6-10 (a) A race car moves around a flat curved track at constant speed $v$. The frictional force $\vec{f}_{s}$ provides the necessary centripetal force along a radial axis $r$. (b) A free-body diagram (not to scale) for the car, in the vertical plane containing $r$.

Additional examples, video, and practice available at WileyPLUS

## Car in banked circular turn

Curved portions of highways are always banked (tilted) to prevent cars from sliding off the highway. When a highway is dry, the frictional force between the tires and the road surface may be enough to prevent sliding. When the highway is wet, however, the frictional force may be negligible, and banking is then essential. Figure 6-11a represents a car of mass $m$ as it moves at a constant speed $v$ of $20 \mathrm{~m} / \mathrm{s}$ around a banked circular track of radius $R=190 \mathrm{~m}$. (It is a normal car, rather than a race car, which means any vertical force from the passing air is negligible.) If the frictional force from the track is negligible, what bank angle $\theta$ prevents sliding?

## KEY IDEAS

Here the track is banked so as to tilt the normal force $\vec{F}_{N}$ on the car toward the center of the circle (Fig. 6-11b). Thus, $\vec{F}_{N}$ now has a centripetal component of magnitude $F_{N r}$, directed inward along a radial axis $r$. We want to find the value of the bank angle $\theta$ such that this centripetal component keeps the car on the circular track without need of friction.

Radial calculation: As Fig. 6-11b shows (and as you should verify), the angle that force $\vec{F}_{N}$ makes with the vertical is equal to the bank angle $\theta$ of the track. Thus, the radial component $F_{N r}$ is equal to $F_{N} \sin \theta$. We can now write Newton's second law for components along the $r$ axis $\left(F_{\text {net }, r}=m a_{r}\right)$ as

$$
\begin{equation*}
-F_{N} \sin \theta=m\left(-\frac{v^{2}}{R}\right) . \tag{6-23}
\end{equation*}
$$

We cannot solve this equation for the value of $\theta$ because it also contains the unknowns $F_{N}$ and $m$.

Vertical calculations: We next consider the forces and acceleration along the $y$ axis in Fig. 6-11b. The vertical component of the normal force is $F_{N y}=F_{N} \cos \theta$, the gravitational force $\vec{F}_{g}$ on the car has the magnitude $m g$, and the acceleration of the car along the $y$ axis is zero. Thus we can write Newton's second law for components along the $y$ axis $\left(F_{\text {net }, y}=m a_{y}\right)$ as

$$
F_{N} \cos \theta-m g=m(0),
$$

from which

$$
\begin{equation*}
F_{N} \cos \theta=m g . \tag{6-24}
\end{equation*}
$$

Combining results: Equation 6-24 also contains the unknowns $F_{N}$ and $m$, but note that dividing Eq. 6-23 by Eq. 6-24 neatly eliminates both those unknowns. Doing so, replacing $(\sin \theta) /(\cos \theta)$ with $\tan \theta$, and solving for $\theta$ then yield

$$
\begin{aligned}
\theta & =\tan ^{-1} \frac{v^{2}}{g R} \\
& =\tan ^{-1} \frac{(20 \mathrm{~m} / \mathrm{s})^{2}}{\left(9.8 \mathrm{~m} / \mathrm{s}^{2}\right)(190 \mathrm{~m})}=12^{\circ} .
\end{aligned}
$$

(Answer)


Fig. 6-11 (a) A car moves around a curved banked road at constant speed $v$. The bank angle is exaggerated for clarity. (b) A free-body diagram for the car, assuming that friction between tires and road is zero and that the car lacks negative lift. The radially inward component $F_{N r}$ of the normal force (along radial axis $r$ ) provides the necessary centripetal force and radial acceleration.

## REVIEW \& SUMMARY

Friction When a force $\vec{F}$ tends to slide a body along a surface, a frictional force from the surface acts on the body. The frictional force is parallel to the surface and directed so as to oppose the sliding. It is due to bonding between the body and the surface.

If the body does not slide, the frictional force is a static frictional force $\vec{f}_{s}$. If there is sliding, the frictional force is a kinetic frictional force $\vec{f}_{k}$.

1. If a body does not move, the static frictional force $\vec{f}_{s}$ and the component of $\vec{F}$ parallel to the surface are equal in magnitude, and $\vec{f}_{s}$ is directed opposite that component. If the component increases, $f_{s}$ also increases.
2. The magnitude of $\vec{f}_{s}$ has a maximum value $f_{s, \text { max }}$ given by

$$
\begin{equation*}
f_{s, \max }=\mu_{s} F_{N}, \tag{6-1}
\end{equation*}
$$

where $\mu_{s}$ is the coefficient of static friction and $F_{N}$ is the magnitude of the normal force. If the component of $\vec{F}$ parallel to the surface exceeds $f_{s, \text { max }}$, the body slides on the surface.
3. If the body begins to slide on the surface, the magnitude of the frictional force rapidly decreases to a constant value $f_{k}$ given by

$$
\begin{equation*}
f_{k}=\mu_{k} F_{N}, \tag{6-2}
\end{equation*}
$$

where $\mu_{k}$ is the coefficient of kinetic friction.
Drag Force When there is relative motion between air (or some other fluid) and a body, the body experiences a drag force $\vec{D}$ that opposes the relative motion and points in the direction in which the fluid flows relative to the body. The magnitude of $\vec{D}$ is
related to the relative speed $v$ by an experimentally determined drag coefficient $C$ according to

$$
\begin{equation*}
D=\frac{1}{2} C \rho A v^{2} \tag{6-14}
\end{equation*}
$$

where $\rho$ is the fluid density (mass per unit volume) and $A$ is the effective cross-sectional area of the body (the area of a cross section taken perpendicular to the relative velocity $\vec{v}$ ).

Terminal Speed When a blunt object has fallen far enough through air, the magnitudes of the drag force $\vec{D}$ and the gravitational force $\vec{F}_{g}$ on the body become equal. The body then falls at a constant terminal speed $v_{t}$ given by

$$
\begin{equation*}
v_{t}=\sqrt{\frac{2 F_{g}}{C \rho A}} . \tag{6-16}
\end{equation*}
$$

Uniform Circular Motion If a particle moves in a circle or a circular arc of radius $R$ at constant speed $v$, the particle is said to be in uniform circular motion. It then has a centripetal acceleration $\vec{a}$ with magnitude given by

$$
\begin{equation*}
a=\frac{v^{2}}{R} \tag{6-17}
\end{equation*}
$$

This acceleration is due to a net centripetal force on the particle, with magnitude given by

$$
\begin{equation*}
F=\frac{m v^{2}}{R} \tag{6-18}
\end{equation*}
$$

where $m$ is the particle's mass. The vector quantities $\vec{a}$ and $\vec{F}$ are directed toward the center of curvature of the particle's path.

1 In Fig. 6-12, if the box is stationary and the angle $\theta$ between the horizontal and force $\vec{F}$ is increased somewhat, do the following quantities increase, decrease, or remain the same: (a) $F_{x}$; (b) $f_{s}$; (c) $F_{N} ;$ (d) $f_{s, \text { max }}$ ? (e) If, instead, the box is sliding and $\theta$ is increased, does the magnitude of the frictional force on the box increase, decrease, or remain the same?


Fig. 6-12 Question 1.

2 Repeat Question 1 for force $\vec{F}$ angled upward instead of downward as drawn.
3 In Fig. 6-13, horizontal force $\vec{F}_{1}$ of magnitude 10 N is applied to a box on a floor, but the box does not slide. Then, as the magnitude of vertical force $\vec{F}_{2}$ is increased from zero, do the following quantities increase, decrease, or stay the same: (a) the magnitude of the frictional force $\vec{f}_{s}$ on the box; (b) the magnitude of the normal force $\vec{F}_{N}$ on the box from the floor; (c) the maximum value $f_{s, \text { max }}$ of
the magnitude of the static frictional force on the box? (d) Does the box eventually slide?


Fig. 6-13 Question 3.

4 In three experiments, three different horizontal forces are applied to the same block lying on the same countertop. The force magnitudes are $F_{1}=12 \mathrm{~N}, F_{2}=8 \mathrm{~N}$, and $F_{3}=4 \mathrm{~N}$. In each experiment, the block remains stationary in spite of the applied force. Rank the forces according to (a) the magnitude $f_{s}$ of the static frictional force on the block from the countertop and (b) the maximum value $f_{s, \text { max }}$ of that force, greatest first.
5 If you press an apple crate against a wall so hard that the crate cannot slide down the wall, what is the direction of (a) the static frictional force $\vec{f}_{s}$ on the crate from the wall and (b) the normal
force $\vec{F}_{N}$ on the crate from the wall? If you increase your push, what happens to (c) $f_{s}$, (d) $F_{N}$, and (e) $f_{s, \text { max }}$ ?

6 In Fig. 6-14, a block of mass $m$ is held stationary on a ramp by the frictional force on it from the ramp. A force $\vec{F}$, directed up the ramp, is then applied to the block and gradu-


Fig. 6-14 Question 6. ally increased in magnitude from zero. During the increase, what happens to the direction and magnitude of the frictional force on the block?
7 Reconsider Question 6 but with the force $\vec{F}$ now directed down the ramp. As the magnitude of $\vec{F}$ is increased from zero, what happens to the direction and magnitude of the frictional force on the block?
8 In Fig. 6-15, a horizontal force of 100 N is to be applied to a 10 kg slab that is initially stationary on a frictionless floor, to accelerate the slab. A 10 kg block lies on top of the slab; the coefficient of friction $\mu$ between the block and the slab is not known, and the block might slip. (a) Considering that possibility, what is the pos-


Fig. 6-15 Question 8.
sible range of values for the magnitude of the slab's acceleration $a_{\text {slab }}$ ? (Hint: You don't need written calculations; just consider extreme values for $\mu$.) (b) What is the possible range for the magnitude $a_{\text {block }}$ of the block's acceleration?
9 Figure 6-16 shows the path of a park ride that travels at constant speed through five circular arcs of radii $R_{0}, 2 R_{0}$, and $3 R_{0}$. Rank the arcs according to the magnitude of the centripetal force on a rider traveling in the arcs, greatest first.


Fig. 6-16 Question 9 . $10 \Longrightarrow$ In 1987, as a Halloween stunt, two sky divers passed a pumpkin back and forth between them while they were in free fall just west of Chicago. The stunt was great fun until the last sky diver with the pumpkin opened his parachute. The pumpkin broke free from his grip, plummeted about 0.5 km , ripped through the roof of a house, slammed into the kitchen floor, and splattered all over the newly remodeled kitchen. From the sky diver's viewpoint and from the pumpkin's viewpoint, why did the sky diver lose control of the pumpkin?
11 A person riding a Ferris wheel moves through positions at (1) the top, (2) the bottom, and (3) midheight. If the wheel rotates at a constant rate, rank these three positions according to (a) the magnitude of the person's centripetal acceleration, (b) the magnitude of the net centripetal force on the person, and (c) the magnitude of the normal force on the person, greatest first.

## sec. 6-3 Properties of Friction

-1 The floor of a railroad flatcar is loaded with loose crates having a coefficient of static friction of 0.25 with the floor. If the train is initially moving at a speed of $48 \mathrm{~km} / \mathrm{h}$, in how short a distance can the train be stopped at constant acceleration without causing the crates to slide over the floor?
-2 In a pickup game of dorm shuffleboard, students crazed by final exams use a broom to propel a calculus book along the dorm hallway. If the 3.5 kg book is pushed from rest through a distance of 0.90 m by the horizontal 25 N force from the broom and then has a speed of $1.60 \mathrm{~m} / \mathrm{s}$, what is the coefficient of kinetic friction between the book and floor?
-3 SSM Www A bedroom bureau with a mass of 45 kg , including drawers and clothing, rests on the floor. (a) If the coefficient of static friction between the bureau and the floor is 0.45 , what is the magnitude of the minimum horizontal force that a person must apply to start the bureau moving? (b) If the drawers and clothing, with 17 kg mass, are removed before the bureau is pushed, what is the new minimum magnitude?
-4 A slide-loving pig slides down a certain $35^{\circ}$ slide in twice the time it would take to slide down a frictionless $35^{\circ}$ slide. What is the coefficient of kinetic friction between the pig and the slide?
-5 ©0 A 2.5 kg block is initially at rest on a horizontal surface. A horizontal force $\vec{F}$ of magnitude 6.0 N and a vertical force $\vec{P}$ are then applied to the block (Fig. 6-17). The coefficients of friction for the block and surface are $\mu_{s}=0.40$ and $\mu_{k}=0.25$. Determine the magnitude of the frictional force acting on the block if the magnitude of $\vec{P}$ is (a) 8.0 N , (b) 10 N , and (c) 12 N .


Fig. 6-17 Problem 5.
-6 A baseball player with mass $m=79 \mathrm{~kg}$, sliding into second base, is retarded by a frictional force of magnitude 470 N . What is
the coefficient of kinetic friction $\mu_{k}$ between the player and the ground?
-7 SSM ILW A person pushes horizontally with a force of 220 N on a 55 kg crate to move it across a level floor. The coefficient of kinetic friction is 0.35 . What is the magnitude of (a) the frictional force and (b) the crate's acceleration?
$\bullet 8$ The mysterious sliding stones. Along the remote Racetrack Playa in Death Valley, California, stones sometimes gouge out prominent trails in the desert floor, as if the stones had been migrating (Fig. 6-18). For years curiosity mounted about why the stones moved. One explanation was that strong winds during occasional rainstorms would drag the rough stones over ground softened by rain. When the desert dried out, the trails behind the stones were hard-baked in place. According to measurements, the coefficient of kinetic friction between the stones and the wet playa ground is about 0.80 . What horizontal force must act on a 20 kg stone (a typical mass) to maintain the stone's motion once a gust has started it moving? (Story continues with Problem 37.)


Fig. 6-18 Problem 8. What moved the stone? (Jerry Schad/ Photo Researchers)
-9 ©0 A 3.5 kg block is pushed along a horizontal floor by a force $\vec{F}$ of magnitude 15 N at an angle $\theta=40^{\circ}$ with the horizontal (Fig. 6-19). The coefficient of kinetic friction between the block and the floor is 0.25 . Calculate the magnitudes of (a) the frictional force on the block from the floor and (b) the block's acceleration.
-10 Figure 6-20 shows an initially stationary block of mass $m$ on a floor. A force of magnitude 0.500 mg is then applied at upward angle $\theta=20^{\circ}$. What is the magnitude of the acceleration of the block across the floor if the friction coefficients are (a) $\mu_{s}=0.600$ and $\mu_{k}=0.500$ and (b) $\mu_{s}=0.400$ and $\mu_{k}=0.300$ ?


Fig. 6-19
Problems 9 and 32.


Fig. 6-20 Problem 10.
-11 SSM A 68 kg crate is dragged across a floor by pulling on a rope attached to the crate and inclined $15^{\circ}$ above the horizontal. (a) If the coefficient of static friction is 0.50 , what minimum force magnitude is required from the rope to start the crate moving? (b) If $\mu_{k}=0.35$, what is the magnitude of the initial acceleration of the crate?
-12 In about 1915, Henry Sincosky of Philadelphia suspended himself from a rafter by gripping the rafter with the thumb of each hand on one side and the fingers on the opposite side (Fig. 6-21). Sincosky's mass was 79 kg . If the coefficient of static friction between hand and rafter was 0.70 , what was the least magnitude of the normal force on the rafter from each thumb or opposite fingers? (After suspending himself, Sincosky chinned himself on the rafter and then moved hand-over-hand along the rafter. If you do not think Sincosky's grip was remarkable, try to repeat his stunt.)
-13 A worker pushes horizontally on a 35 kg crate with a force of magnitude 110 N . The coefficient of static friction between the crate and the floor is 0.37 . (a) What is the value of $f_{s, \text { max }}$ under the circumstances? (b) Does the crate move? (c) What is the frictional force on the crate from the floor? (d) Suppose, next, that a second worker pulls directly upward on the crate to help out. What is the least vertical pull that will allow the first worker's 110 N push to move the crate? (e) If,


Fig. 6-21 Problem 12. instead, the second worker pulls horizontally to help out, what is the least pull that will get the crate moving?
-14 Figure 6-22 shows the cross section of a road cut into the side of a mountain. The solid line $A A^{\prime}$ represents a weak bedding plane along which sliding is possible. Block $B$ directly above the highway is separated from uphill rock by a large crack (called a joint), so that only friction between the block and the bedding plane prevents sliding. The mass of the block is $1.8 \times 10^{7} \mathrm{~kg}$, the dip angle $\theta$ of the bedding plane is $24^{\circ}$, and the coefficient of static friction between block and plane is 0.63 . (a) Show that the block will not slide under these circumstances. (b) Next, water seeps into the joint and expands upon freezing, exerting on the block a force $\vec{F}$ parallel to $A A^{\prime}$. What minimum value of force magnitude $F$ will trigger a slide down the plane?


Fig. 6-22 Problem 14.
-15 The coefficient of static friction between Teflon and scrambled eggs is about 0.04 . What is the smallest angle from the horizontal that will cause the eggs to slide across the bottom of a Teflon-coated skillet?
-11 A loaded penguin sled weighing 80 N rests on a plane inclined at angle $\theta=20^{\circ}$ to the horizontal (Fig. 6-23). Between the sled and the plane, the coefficient of static friction is 0.25 , and the coefficient of kinetic friction is 0.15 . (a) What is the least magnitude of the force $\vec{F}$, parallel to the plane, that will prevent the sled from slipping down the plane? (b) What is the minimum magnitude $F$ that will start the sled moving up the plane? (c) What value of $F$ is required to move the sled up the plane at constant velocity?


Fig. 6-23 Problems 16 and 22.
-•17 In Fig. 6-24, a force $\vec{P}$ acts on a block weighing 45 N . The block is initially at rest on a plane inclined at angle $\theta=15^{\circ}$ to the horizontal. The positive direction of the $x$ axis is up the plane. The coefficients of friction between block and plane are $\mu_{s}=0.50$ and $\mu_{k}=0.34$. In unit-vector notation, what is the frictional force on the block from the plane when $\vec{P}$ is (a) $(-5.0 \mathrm{~N}) \hat{\mathrm{i}}$, (b) $(-8.0 \mathrm{~N}) \hat{\mathrm{i}}$, and (c) $(-15 \mathrm{~N}) \hat{\mathrm{i}}$ ?


Fig. 6-24 Problem 17.
$\bullet 18$ You testify as an expert witness in a case involving an accident in which car $A$ slid into the rear of car $B$, which was stopped at a red light along a road headed down a hill (Fig. 6-25). You find that the slope of the hill is $\theta=12.0^{\circ}$, that the cars were separated by distance $d=24.0 \mathrm{~m}$ when the driver of car $A$ put the car into a slide (it lacked any automatic anti-brake-lock system), and that the speed of car $A$ at the onset of braking was $v_{0}=18.0 \mathrm{~m} / \mathrm{s}$. With what speed did car $A$ hit car $B$ if the coefficient of kinetic friction was (a) 0.60 (dry road surface) and (b) 0.10 (road surface covered with wet leaves)?


Fig. 6-25 Problem 18.

- 19 A 12 N horizontal force $\vec{F}$ pushes a block weighing 5.0 N against a vertical wall (Fig. 6-26). The coefficient of static friction between the wall and the block is 0.60 , and the coefficient of kinetic friction is 0.40 . Assume that the block is notot
moving initially. (a) Will the block move? (b) In unit-vector notation, what is the force on the block from the wall?
$\bullet 020$ (60 In Fig. 6-27, a box of Cheerios (mass $m_{C}=1.0 \mathrm{~kg}$ ) and a box of Wheaties (mass $m_{W}=3.0 \mathrm{~kg}$ ) are accelerated across a horizontal surface by a horizontal force $\vec{F}$ applied to the Cheerios box. The magnitude of the frictional force on the Cheerios box is 2.0 N , and the magnitude of the frictional force on the Wheaties box is 4.0 N . If the magnitude of $\vec{F}$ is 12 N , what is the magnitude of the force on the Wheaties box from the Cheerios box?


Fig. 6-27 Problem 20.
-221 An initially stationary box of sand is to be pulled across a floor by means of a cable in which the tension should not exceed 1100 N . The coefficient of static friction between the box and the floor is 0.35 . (a) What should be the angle between the cable and the horizontal in order to pull the greatest possible amount of sand, and (b) what is the weight of the sand and box in that situation?
$\bullet 022$ ©0 In Fig. 6-23, a sled is held on an inclined plane by a cord pulling directly up the plane. The sled is to be on the verge of moving up the plane. In Fig. 6-28, the magnitude $F$ required of the cord's force on the sled is plotted versus a range of values for the coefficient of static friction $\mu_{s}$ between sled and plane: $F_{1}=2.0 \mathrm{~N}$, $F_{2}=5.0 \mathrm{~N}$, and $\mu_{2}=0.50$. At what angle $\theta$ is the plane inclined?


Fig. 6-28 Problem 22.
-023 When the three blocks in Fig. 6-29 are released from rest, they accelerate with a magnitude of 0.500 $\mathrm{m} / \mathrm{s}^{2}$. Block 1 has mass $M$, block 2 has $2 M$, and block 3 has $2 M$. What is the coefficient of kinetic friction between block 2 and the table?

- 24 A 4.10 kg block is pushed along a floor by a constant applied force that is horizontal and has a magnitude of 40.0 N . Figure 6-30 gives the block's speed $v$ versus time $t$ as the block moves along an $x$ axis on the floor. The scale of the figure's vertical axis is set by $v_{s}=5.0$ $\mathrm{m} / \mathrm{s}$. What is the coefficient of kinetic friction between the block and the floor?


Fig. 6-29 Problem 23.


Fig. 6-30 Problem 24.
$\bullet 25$ ssm www Block $B$ in Fig 6-31 weighs 711 N . The coefficient of static friction between block and table is 0.25 ; angle $\theta$ is $30^{\circ}$; assume that the cord between $B$ and the knot is horizontal. Find the maximum weight of block $A$ for which the system will be stationary.
-26 60 Figure 6-32 shows three crates being pushed over a concrete floor by a horizontal force $\vec{F}$ of magnitude 440 N . The masses of the crates are $m_{1}=30.0 \mathrm{~kg}, m_{2}=10.0$ kg , and $m_{3}=20.0 \mathrm{~kg}$. The coefficient of kinetic friction between the floor and each of the crates is 0.700 . (a) What is the magnitude $F_{32}$ of the force on crate 3 from crate 2? (b) If the crates then slide onto a polished floor, where the coefficient of kinetic friction is less than 0.700 , is magnitude $F_{32}$ more than, less than, or the same as it was when the coefficient was 0.700 ?
$\bullet 27$ Body $A$ in Fig. 6-33 weighs 102 N , and body $B$ weighs 32 N . The coefficients of friction between $A$ and the incline are $\mu_{s}=0.56$ and $\mu_{k}=0.25$. Angle $\theta$ is $40^{\circ}$. Let the positive direction of an $x$ axis be up the incline. In unit-vector notation, what is the acceleration of $A$ if $A$ is initially (a) at rest, (b) moving up the incline, and (c) moving down the incline?
-28 In Fig. 6-33, two blocks are connected over a pulley. The mass of block $A$ is 10 kg , and the coefficient of kinetic friction between $A$ and the incline is 0.20 . Angle $\theta$ of the incline is $30^{\circ}$. Block $A$ slides down the incline at constant speed. What is the mass of block $B$ ?
-29 In Fig. 6-34, blocks $A$ and $B$ have weights of 44 N and 22 N , respectively. (a) Determine the minimum weight of block $C$ to keep $A$ from sliding if $\mu_{s}$ between $A$ and the table is 0.20 . (b) Block $C$ suddenly is lifted off $A$. What is the acceleration of block $A$ if $\mu_{k}$ between $A$ and the table is 0.15 ?


Fig. 6-34 Problem 29.
-•30 A toy chest and its contents have a combined weight of 180 N . The coefficient of static friction between toy chest and floor is 0.42. The child in Fig. 6-35 attempts to move the chest across the floor by pulling on an attached rope. (a) If $\theta$ is $42^{\circ}$, what is the mag-
nitude of the force $\vec{F}$ that the child must exert on the rope to put the chest on the verge of moving? (b) Write an expression for the magnitude $F$ required to put the chest on the verge of moving as a function of the angle $\theta$. Determine (c) the value of $\theta$ for which $F$ is a minimum and (d) that minimum magnitude.


Fig. 6-35 Problem 30.

- 31 SSm Two blocks, of weights 3.6 N and 7.2 N , are connected by a massless string and slide down a $30^{\circ}$ inclined plane. The coefficient of kinetic friction between the lighter block and the plane is 0.10 , and the coefficient between the heavier block and the plane is 0.20 . Assuming that the lighter block leads, find (a) the magnitude of the acceleration of the blocks and (b) the tension in the taut string.
- 32 (60 A block is pushed across a floor by a constant force that is applied at downward angle $\theta$ (Fig. 6-19). Figure 6-36 gives the acceleration magnitude $a$ versus a range of values for the coefficient of kinetic friction $\mu_{k}$ between block and floor: $a_{1}=3.0 \mathrm{~m} / \mathrm{s}^{2}, \mu_{k 2}=$ 0.20 , and $\mu_{k 3}=0.40$. What is the value of $\theta$ ?


Fig. 6-36 Problem 32.
-0033 SSM A 1000 kg boat is traveling at $90 \mathrm{~km} / \mathrm{h}$ when its engine is shut off. The magnitude of the frictional force $\vec{f}_{k}$ between boat and water is proportional to the speed $v$ of the boat: $f_{k}=70 v$, where $v$ is in meters per second and $f_{k}$ is in newtons. Find the time required for the boat to slow to $45 \mathrm{~km} / \mathrm{h}$.
-•034 ©50 In Fig. 6-37, a slab of mass $m_{1}=40 \mathrm{~kg}$ rests on a frictionless floor, and a block of mass $m_{2}=10 \mathrm{~kg}$ rests on top of the slab. Between block and slab, the coefficient of static friction is 0.60 , and the coefficient of kinetic friction is 0.40 . A horizontal force $\vec{F}$ of magnitude 100 N begins to pull directly on the block, as shown. In unit-vector notation, what are the resulting accelerations of (a) the block and (b) the slab?


Fig. 6-37 Problem 34.
-•035 ILW The two blocks ( $m=16 \mathrm{~kg}$ and $M=88 \mathrm{~kg}$ ) in Fig. 6-38 are not attached to each other. The coefficient of static friction between the blocks is $\mu_{s}=0.38$, but the surface beneath the larger block is frictionless. What is the minimum magnitude of the horizontal force $\vec{F}$ required to keep the smaller block from slipping down the larger block?


Fig. 6-38 Problem 35.

## sec. 6-4 The Drag Force and Terminal Speed

-36 The terminal speed of a sky diver is $160 \mathrm{~km} / \mathrm{h}$ in the spreadeagle position and $310 \mathrm{~km} / \mathrm{h}$ in the nosedive position. Assuming that the diver's drag coefficient $C$ does not change from one position to the other, find the ratio of the effective cross-sectional area $A$ in the slower position to that in the faster position.
$\bullet 37 \Longrightarrow$ Continuation of Problem 8. Now assume that Eq. 6-14 gives the magnitude of the air drag force on the typical 20 kg stone, which presents to the wind a vertical cross-sectional area of 0.040 $\mathrm{m}^{2}$ and has a drag coefficient $C$ of 0.80 . Take the air density to be $1.21 \mathrm{~kg} / \mathrm{m}^{3}$, and the coefficient of kinetic friction to be 0.80 . (a) In kilometers per hour, what wind speed $V$ along the ground is needed to maintain the stone's motion once it has started moving? Because winds along the ground are retarded by the ground, the wind speeds reported for storms are often measured at a height of 10 m . Assume wind speeds are 2.00 times those along the ground. (b) For your answer to (a), what wind speed would be reported for the storm? (c) Is that value reasonable for a high-speed wind in a storm? (Story continues with Problem 65.)

- 33 Assume Eq. 6-14 gives the drag force on a pilot plus ejection seat just after they are ejected from a plane traveling horizontally at $1300 \mathrm{~km} / \mathrm{h}$. Assume also that the mass of the seat is equal to the mass of the pilot and that the drag coefficient is that of a sky diver. Making a reasonable guess of the pilot's mass and using the appropriate $v_{t}$ value from Table 6-1, estimate the magnitudes of (a) the drag force on the pilot + seat and (b) their horizontal deceleration (in terms of $g$ ), both just after ejection. (The result of (a) should indicate an engineering requirement: The seat must include a protective barrier to deflect the initial wind blast away from the pilot's head.)
- 39 Calculate the ratio of the drag force on a jet flying at 1000 $\mathrm{km} / \mathrm{h}$ at an altitude of 10 km to the drag force on a prop-driven transport flying at half that speed and altitude. The density of air is $0.38 \mathrm{~kg} / \mathrm{m}^{3}$ at 10 km and $0.67 \mathrm{~kg} / \mathrm{m}^{3}$ at 5.0 km . Assume that the airplanes have the same effective cross-sectional area and drag coefficient $C$.
$\because 40$ In downhill speed skiing a skier is retarded by both the air drag force on the body and the kinetic frictional force on the skis. (a) Suppose the slope angle is $\theta=40.0^{\circ}$, the snow is dry snow with a coefficient of kinetic friction $\mu_{k}=0.0400$, the mass of the skier and equipment is $m=85.0 \mathrm{~kg}$, the cross-sectional area of the (tucked) skier is $A=1.30 \mathrm{~m}^{2}$, the drag coefficient is $C=0.150$, and the air density is $1.20 \mathrm{~kg} / \mathrm{m}^{3}$. (a) What is the terminal speed? (b) If a skier can vary $C$ by a slight amount $d C$ by adjusting, say, the hand positions, what is the corresponding variation in the terminal speed?


## sec. 6-5 Uniform Circular Motion

-41 A cat dozes on a stationary merry-go-round, at a radius of 5.4 m from the center of the ride. Then the operator turns on the ride
and brings it up to its proper turning rate of one complete rotation every 6.0 s . What is the least coefficient of static friction between the cat and the merry-go-round that will allow the cat to stay in place, without sliding?
-42 Suppose the coefficient of static friction between the road and the tires on a car is 0.60 and the car has no negative lift. What speed will put the car on the verge of sliding as it rounds a level curve of 30.5 m radius?
-43 ILW What is the smallest radius of an unbanked (flat) track around which a bicyclist can travel if her speed is $29 \mathrm{~km} / \mathrm{h}$ and the $\mu_{s}$ between tires and track is 0.32 ?
-44 During an Olympic bobsled run, the Jamaican team makes a turn of radius 7.6 m at a speed of $96.6 \mathrm{~km} / \mathrm{h}$. What is their acceleration in terms of $g$ ?
$\bullet 45$ SSM ILW A student of weight 667 N rides a steadily rotating Ferris wheel (the student sits upright). At the highest point, the magnitude of the normal force $\vec{F}_{N}$ on the student from the seat is 556 N . (a) Does the student feel "light" or "heavy" there? (b) What is the magnitude of $\vec{F}_{N}$ at the lowest point? If the wheel's speed is doubled, what is the magnitude $F_{N}$ at the (c) highest and (d) lowest point?
صッ46 A police officer in hot pursuit drives her car through a circular turn of radius 300 m with a constant speed of $80.0 \mathrm{~km} / \mathrm{h}$. Her mass is 55.0 kg . What are (a) the magnitude and (b) the angle (relative to vertical) of the net force of the officer on the car seat? (Hint: Consider both horizontal and vertical forces.)
$\bullet 47 \sim$ A circular-motion addict of mass 80 kg rides a Ferris wheel around in a vertical circle of radius 10 m at a constant speed of $6.1 \mathrm{~m} / \mathrm{s}$. (a) What is the period of the motion? What is the magnitude of the normal force on the addict from the seat when both go through (b) the highest point of the circular path and (c) the lowest point?
$\because 48$ A roller-coaster car has a mass of 1200 kg when fully loaded with passengers. As the car passes over the top of a circular hill of radius 18 m , its speed is not changing. At the top of the hill, what are the (a) magnitude $F_{N}$ and (b) direction (up or down) of the normal force on the car from the track if the car's speed is $v=11 \mathrm{~m} / \mathrm{s}$ ? What are (c) $F_{N}$ and (d) the direction if $v=$ $14 \mathrm{~m} / \mathrm{s}$ ?
-थ49 In Fig. 6-39, a car is driven at constant speed over a circular hill and then into a circular valley with the same radius. At the top of the hill, the normal force on the driver from the car seat is 0 . The driver's mass is 70.0 kg . What is the magnitude of the normal force on the driver from the seat when the car passes through the bottom of the valley?


Fig. 6-39 Problem 49.

- 50 An 85.0 kg passenger is made to move along a circular path of radius $r=3.50 \mathrm{~m}$ in uniform circular motion. (a) Figure 6-40a is a plot of the required magnitude $F$ of the net centripetal force for a range of possible values of the passenger's speed $v$. What is the
plot's slope at $v=8.30 \mathrm{~m} / \mathrm{s}$ ? (b) Figure $6-40 b$ is a plot of $F$ for a range of possible values of $T$, the period of the motion. What is the plot's slope at $T=2.50 \mathrm{~s}$ ?


Fig. 6-40 Problem 50.
-051 SSM Www An airplane is flying in a horizontal circle at a speed of $480 \mathrm{~km} / \mathrm{h}$ (Fig. 6-41). If its wings are tilted at angle $\theta=40^{\circ}$ to the horizontal, what is the radius of the circle in which the plane is flying? Assume that the required force is provided entirely by an "aerodynamic lift" that is perpendicular to the wing surface.


Fig. 6-41 Problem 51.
-052 An amusement park ride consists of a car moving in a vertical circle on the end of a rigid boom of negligible mass. The combined weight of the car and riders is 5.0 kN , and the circle's radius is 10 m . At the top of the circle, what are the (a) magnitude $F_{B}$ and (b) direction (up or down) of the force on the car from the boom if the car's speed is $v=5.0 \mathrm{~m} / \mathrm{s}$ ? What are (c) $F_{B}$ and (d) the direction if $v=12 \mathrm{~m} / \mathrm{s}$ ?
-०53 An old streetcar rounds a flat corner of radius 9.1 m , at 16 $\mathrm{km} / \mathrm{h}$. What angle with the vertical will be made by the loosely hanging hand straps?
-054 $\#$ In designing circular rides for amusement parks, mechanical engineers must consider how small variations in certain parameters can alter the net force on a passenger. Consider a passenger of mass $m$ riding around a horizontal circle of radius $r$ at speed $v$. What is the variation $d F$ in the net force magnitude for (a) a variation $d r$ in the radius with $v$ held constant, (b) a variation $d v$ in the speed with $r$ held constant, and (c) a variation $d T$ in the period with $r$ held constant?
-•55 A bolt is threaded onto one end of a thin horizontal rod, and the rod is then rotated horizontally about its other end. An engineer monitors the motion by flashing a strobe lamp onto the rod and bolt, adjusting the strobe rate until the bolt appears to be in the same eight places during each full rotation of the rod (Fig. 6-42). The
strobe rate is 2000 flashes per second; the bolt has mass 30 g and is at radius 3.5 cm . What is the magnitude of the force on the bolt from the rod?
-•56 ©0 A banked circular highway curve is designed for traffic moving at $60 \mathrm{~km} / \mathrm{h}$. The radius of the curve is 200 m . Traffic is moving along the highway at $40 \mathrm{~km} / \mathrm{h}$ on a rainy day. What is the minimum coefficient of friction between tires and road that will allow cars to take the turn without sliding off the road? (Assume the cars do not have negative lift.)
-•57 ©0 A puck of mass $m=1.50$ kg slides in a circle of radius $r=20.0 \mathrm{~cm}$ on a frictionless table while attached to a hanging cylinder of mass $M=2.50 \mathrm{~kg}$ by means of a cord that extends through a hole in the table (Fig. 6-43). What speed keeps the cylinder at rest?
$\bullet 58$ Brake or turn? Figure 6-44 depicts an overhead view of a car's path as the car travels toward a wall. Assume that the driver begins to brake the car when the distance to the wall is $d=107 \mathrm{~m}$, and take the car's mass as $m=1400 \mathrm{~kg}$, its initial speed as $v_{0}=35 \mathrm{~m} / \mathrm{s}$, and the coefficient of static friction as $\mu_{s}=$ 0.50 . Assume that the car's weight is distributed evenly on the four wheels, even during braking. (a) What magnitude of static friction is needed (between tires and road) to stop the car just as it reaches the wall? (b) What is the maximum pos-


Fig. 6-43
Problem 57.


Fig. 6-44 Problem 58. sible static friction $f_{s, \max }$ ? (c) If the coefficient of kinetic friction between the (sliding) tires and the road is $\mu_{k}=0.40$, at what speed will the car hit the wall? To avoid the crash, a driver could elect to turn the car so that it just barely misses the wall, as shown in the figure. (d) What magnitude of frictional force would be required to keep the car in a circular path of radius $d$ and at the given speed $v_{0}$, so that the car moves in a quarter circle and then parallel to the wall? (e) Is the required force less than $f_{s, \text { max }}$ so that a circular path is possible?
-0559 SSM ILW In Fig. 6-45, a 1.34 kg ball is connected by means of two massless strings, each of length $L=$ 1.70 m , to a vertical, rotating rod. The strings are tied to the rod with separation $d=1.70 \mathrm{~m}$ and are taut. The tension in the upper string is 35 N . What are the (a) tension in the lower string, (b) magnitude of the net force $\vec{F}_{\text {net }}$ on the ball, and (c) speed of the ball? (d) What is the direction of $\vec{F}_{\text {net }}$ ?


Fig. 6-45 Problem 59.

## Additional Problems

60 In Fig. 6-46, a box of ant aunts (total mass $m_{1}=1.65 \mathrm{~kg}$ ) and a box of ant uncles (total mass $m_{2}=3.30 \mathrm{~kg}$ ) slide down an inclined plane while attached by a massless rod parallel to the plane. The angle of incline is $\theta=30.0^{\circ}$. The coefficient of kinetic friction between the aunt box and the incline is $\mu_{1}=0.226$; that between the uncle box and the incline is $\mu_{2}=0.113$. Compute (a) the tension in the rod and (b) the magnitude of the common acceleration of the two boxes. (c) How would the answers to (a) and (b) change if the uncles trailed the aunts?
61 SSM A block of mass $m_{t}=4.0$ kg is put on top of a block of mass $m_{b}=5.0 \mathrm{~kg}$. To cause the top block to slip on the bottom one while the bottom one is held fixed, a horizontal force of at least 12 N must be ap-


Fig. 6-47 Problem 61. pled the top


Fig. 6-46 Problem 60.
rock is 1.2 ; between her back and the rock is 0.80 . She has reduced her push against the rock until her back and her shoes are on the verge of slipping. (a) Draw a free-body diagram of her. (b) What is the magnitude of her push against the rock? (c) What fraction of her weight is supported by the frictional force on her shoes?
64 A high-speed railway car goes around a flat, horizontal circle of radius 470 m at a constant speed. The magnitudes of the horizontal and vertical components of the force of the car on a 51.0 kg passenger are 210 N and 500 N , respectively. (a) What is the magnitude of the net force (of all the forces) on the passenger? (b) What is the speed of the car?
$65=$ Continuation of Problems 8 and 37. Another explanation is that the stones move only when the water dumped on the playa during a storm freezes into a large, thin sheet of ice. The stones are trapped in place in the ice. Then, as air flows across the ice during a wind, the air-drag forces on the ice and stones move them both, with the stones gouging out the trails. The magnitude of the air-drag force on this horizontal "ice sail" is given by $D_{\text {ice }}=4 C_{\text {ice }} \rho A_{\text {ice }} v^{2}$, where $C_{\text {ice }}$ is the drag coefficient $\left(2.0 \times 10^{-3}\right), \rho$ is the air density $\left(1.21 \mathrm{~kg} / \mathrm{m}^{3}\right), A_{\text {ice }}$ is the horizontal area of the ice, and $v$ is the wind speed along the ice.

Assume the following: The ice sheet measures 400 m by 500 m by 4.0 mm and has a coefficient of kinetic friction of 0.10 with the ground and a density of $917 \mathrm{~kg} / \mathrm{m}^{3}$. Also assume that 100 stones identical to the one in Problem 8 are trapped in the ice. To maintain the motion of the sheet, what are the required wind speeds (a) near the sheet and (b) at a height of 10 m ? (c) Are these reasonable values for high-speed winds in a storm?
66 ©0 In Fig. 6-50, block 1 of mass $m_{1}=2.0 \mathrm{~kg}$ and block 2 of mass $m_{2}=3.0 \mathrm{~kg}$ are connected by a string of negligible mass and are initially held in place. Block 2 is on a frictionless surface tilted at $\theta=30^{\circ}$. The coefficient of kinetic friction between block 1 and the horizontal surface is 0.25 . The pulley has negligible mass and friction. Once they are released, the blocks move. What then is the tension in the string?


Fig. 6-50 Problem 66.
67 In Fig. 6-51, a crate slides down an inclined right-angled trough. The coefficient of kinetic friction between the crate and the trough is $\mu_{k}$. What is the acceleration of the crate in terms of $\mu_{k}, \theta$, and $g$ ?


Fig. 6-51 Problem 67.

68 Engineering a highway curve. If a car goes through a curve too fast, the car tends to slide out of the curve. For a banked curve with
friction, a frictional force acts on a fast car to oppose the tendency to slide out of the curve; the force is directed down the bank (in the direction water would drain). Consider a circular curve of radius $R=200 \mathrm{~m}$ and bank angle $\theta$, where the coefficient of static friction between tires and pavement is $\mu_{s}$. A car (without negative lift) is driven around the curve as shown in Fig. 6-11. (a) Find an expression for the car speed $v_{\text {max }}$ that puts the car on the verge of sliding out. (b) On the same graph, plot $v_{\max }$ versus angle $\theta$ for the range $0^{\circ}$ to $50^{\circ}$, first for $\mu_{s}=0.60$ (dry pavement) and then for $\mu_{s}=0.050$ (wet or icy pavement). In kilometers per hour, evaluate $v_{\text {max }}$ for a bank angle of $\theta=10^{\circ}$ and for (c) $\mu_{s}=0.60$ and (d) $\mu_{s}=$ 0.050. (Now you can see why accidents occur in highway curves when icy conditions are not obvious to drivers, who tend to drive at normal speeds.)
69 A student, crazed by final exams, uses a force $\vec{P}$ of magnitude 80 N and angle $\theta=70^{\circ}$ to push a 5.0 kg block across the ceiling of his room (Fig. 6-52). If the coefficient of kinetic friction between the block and the ceiling is 0.40 , what is the magnitude of the block's acceleration?


Fig. 6-52 Problem 69.

70 Figure 6-53 shows a conical pendulum, in which the bob (the small object at the lower end of the cord) moves in a horizontal circle at constant speed. (The cord sweeps out a cone as the bob rotates.) The bob has a mass of 0.040 kg , the string has length $L=0.90 \mathrm{~m}$ and negligible mass, and the bob follows a circular path of circumference 0.94 m . What are (a) the tension in the string and (b) the period of the motion?
71 An 8.00 kg block of steel is at rest on a horizontal table. The coefficient of static friction between the block and the table is 0.450 . A force is to be applied to the block. To three significant figures, what is the magnitude of that applied force if it puts the block on the verge of sliding when the force is directed


Fig. 6-53 Problem 70. (a) horizontally, (b) upward at $60.0^{\circ}$ from the horizontal, and (c) downward at $60.0^{\circ}$ from the horizontal?

72 A box of canned goods slides down a ramp from street level into the basement of a grocery store with acceleration $0.75 \mathrm{~m} / \mathrm{s}^{2} \mathrm{di}-$ rected down the ramp. The ramp makes an angle of $40^{\circ}$ with the horizontal. What is the coefficient of kinetic friction between the box and the ramp?
73 In Fig. 6-54, the coefficient of kinetic friction between the block and inclined plane is 0.20 , and angle $\theta$ is $60^{\circ}$. What are the (a) magnitude $a$ and (b) direction (up or down the plane) of the
block's acceleration if the block is sliding down the plane? What are (c) $a$ and (d) the direction if the block is sent sliding up the plane?
74 A 110 g hockey puck sent sliding over ice is stopped in 15 m by the frictional force on it from the ice. (a) If its initial speed is $6.0 \mathrm{~m} / \mathrm{s}$, what is the magnitude of the frictional force? (b) What is the coefficient of friction between the puck and the ice?


Fig. 6-54 Problem 73.

75 A locomotive accelerates a 25 -car train along a level track. Every car has a mass of $5.0 \times 10^{4} \mathrm{~kg}$ and is subject to a frictional force $f=250 v$, where the speed $v$ is in meters per second and the force $f$ is in newtons. At the instant when the speed of the train is 30 $\mathrm{km} / \mathrm{h}$, the magnitude of its acceleration is $0.20 \mathrm{~m} / \mathrm{s}^{2}$. (a) What is the tension in the coupling between the first car and the locomotive? (b) If this tension is equal to the maximum force the locomotive can exert on the train, what is the steepest grade up which the locomotive can pull the train at $30 \mathrm{~km} / \mathrm{h}$ ?
76 A house is built on the top of a hill with a nearby slope at angle $\theta=45^{\circ}$ (Fig. 6-55). An engineering study indicates that the slope angle should be reduced because the top layers of soil along the slope might slip past the lower layers. If the coefficient of static friction between two such layers is 0.5 , what is the least angle $\phi$ through which the present slope should be reduced to prevent slippage?


Fig. 6-55 Problem 76.

77 What is the terminal speed of a 6.00 kg spherical ball that has a radius of 3.00 cm and a drag coefficient of 1.60 ? The density of the air through which the ball falls is $1.20 \mathrm{~kg} / \mathrm{m}^{3}$.
78 A student wants to determine the coefficients of static friction and kinetic friction between a box and a plank. She places the box on the plank and gradually raises one end of the plank. When the angle of inclination with the horizontal reaches $30^{\circ}$, the box starts to slip, and it then slides 2.5 m down the plank in 4.0 s at constant acceleration. What are (a) the coefficient of static friction and (b) the coefficient of kinetic friction between the box and the plank?
79 ssm Block $A$ in Fig. 6-56 has mass $m_{A}=4.0 \mathrm{~kg}$, and block $B$ has mass $m_{B}=2.0 \mathrm{~kg}$. The coefficient of kinetic friction between block $B$


Fig. 6-56 Problem 79.
and the horizontal plane is $\mu_{k}=0.50$. The inclined plane is frictionless and at angle $\theta=30^{\circ}$. The pulley serves only to change the direction of the cord connecting the blocks. The cord has negligible mass. Find (a) the tension in the cord and (b) the magnitude of the acceleration of the blocks.

80 Calculate the magnitude of the drag force on a missile 53 cm in diameter cruising at $250 \mathrm{~m} / \mathrm{s}$ at low altitude, where the density of air is $1.2 \mathrm{~kg} / \mathrm{m}^{3}$. Assume $C=0.75$.
81 SSM A bicyclist travels in a circle of radius 25.0 m at a constant speed of $9.00 \mathrm{~m} / \mathrm{s}$. The bicycle-rider mass is 85.0 kg . Calculate the magnitudes of (a) the force of friction on the bicycle from the road and (b) the net force on the bicycle from the road.

82 In Fig. 6-57, a stuntman drives a car (without negative lift) over the top of a hill, the cross section of which can be approximated by a circle of radius $R=250 \mathrm{~m}$. What is the greatest speed at which he can drive without the car leaving the road at the top of the hill?


Fig. 6-57 Problem 82.

83 You must push a crate across a floor to a docking bay. The crate weighs 165 N . The coefficient of static friction between crate and floor is 0.510 , and the coefficient of kinetic friction is 0.32 . Your force on the crate is directed horizontally. (a) What magnitude of your push puts the crate on the verge of sliding? (b) With what magnitude must you then push to keep the crate moving at a constant velocity? (c) If, instead, you then push with the same magnitude as the answer to (a), what is the magnitude of the crate's acceleration?
84 In Fig. 6-58, force $\vec{F}$ is applied to a crate of mass $m$ on a floor where the coefficient of static friction between crate and floor is $\mu_{s}$. Angle $\theta$ is initially $0^{\circ}$ but is gradually increased so that the force vector rotates clockwise in the figure. During the rotation, the magnitude $F$ of the force is continuously adjusted so that the crate is always on the verge of sliding. For $\mu_{s}=0.70$, (a) plot the ratio $F / m g$ versus $\theta$ and (b) determine the angle $\theta_{\mathrm{inf}}$ at which the ratio approaches an infinite value. (c) Does lubricating the floor increase or decrease $\theta_{\text {inf }}$, or is the value unchanged? (d) What is $\theta_{\text {inf }}$ for $\mu_{s}=0.60$ ?


Fig. 6-58 Problem 84.

85 In the early afternoon, a car is parked on a street that runs down a steep hill, at an angle of $35.0^{\circ}$ relative to the horizontal. Just then the coefficient of static friction between the tires and the street surface is 0.725 . Later, after nightfall, a sleet storm hits the
area, and the coefficient decreases due to both the ice and a chemical change in the road surface because of the temperature decrease. By what percentage must the coefficient decrease if the car is to be in danger of sliding down the street?
$86=$ A sling-thrower puts a stone $(0.250 \mathrm{~kg})$ in the sling's pouch $(0.010 \mathrm{~kg})$ and then begins to make the stone and pouch move in a vertical circle of radius 0.650 m . The cord between the pouch and the person's hand has negligible mass and will break when the tension in the cord is 33.0 N or more. Suppose the slingthrower could gradually increase the speed of the stone. (a) Will the breaking occur at the lowest point of the circle or at the highest point? (b) At what speed of the stone will that breaking occur?
87 SSM A car weighing 10.7 kN and traveling at $13.4 \mathrm{~m} / \mathrm{s}$ without negative lift attempts to round an unbanked curve with a radius of 61.0 m . (a) What magnitude of the frictional force on the tires is required to keep the car on its circular path? (b) If the coefficient of static friction between the tires and the road is 0.350 , is the attempt at taking the curve successful?
88 In Fig. 6-59, block 1 of mass $m_{1}=2.0 \mathrm{~kg}$ and block 2 of mass $m_{2}=1.0 \mathrm{~kg}$ are connected by a string of negligible mass. Block 2 is pushed by force $\vec{F}$ of magnitude 20 N and angle $\theta=35^{\circ}$. The coefficient of kinetic friction between each block and the horizontal surface is 0.20 . What is the tension in the string?


Fig. 6-59 Problem 88.

89 SSm A filing cabinet weighing 556 N rests on the floor. The coefficient of static friction between it and the floor is 0.68 , and the coefficient of kinetic friction is 0.56 . In four different attempts to move it, it is pushed with horizontal forces of magnitudes (a) 222 N, (b) 334 N , (c) 445 N , and (d) 556 N . For each attempt, calculate the magnitude of the frictional force on it from the floor. (The cabinet is initially at rest.) (e) In which of the attempts does the cabinet move?
90 In Fig. 6-60, a block weighing 22 N is held at rest against a vertical wall by a horizontal force $\vec{F}$ of magnitude 60 N . The coefficient of static friction between the wall and the block is 0.55 , and the coefficient of kinetic friction between them is 0.38 . In six experiments, a second force $\vec{P}$ is applied to the block and directed parallel to the wall with these magnitudes and directions: (a) 34 N , up, (b) 12 N , up, (c) 48 N , up, (d) 62 N , up, (e) 10 N , down, and (f)


Fig. 6-60 Problem 90. 18 N , down. In each experiment, what is the magni- tude of the frictional force on the block? In which does the block move (g) up the wall and (h) down the wall? (i) In which is the frictional force directed down the wall?
91 SSM A block slides with constant velocity down an inclined plane that has slope angle $\theta$. The block is then projected up the same plane with an initial speed $v_{0}$. (a) How far up the plane will it move before coming to rest? (b) After the block comes to rest, will it slide down the plane again? Give an argument to back your answer.

## ** View All Solutions Here **

92 A circular curve of highway is designed for traffic moving at $60 \mathrm{~km} / \mathrm{h}$. Assume the traffic consists of cars without negative lift. (a) If the radius of the curve is 150 m , what is the correct angle of banking of the road? (b) If the curve were not banked, what would be the minimum coefficient of friction between tires and road that would keep traffic from skidding out of the turn when traveling at $60 \mathrm{~km} / \mathrm{h}$ ?
93 A 1.5 kg box is initially at rest on a horizontal surface when at $t=$ 0 a horizontal force $\vec{F}=(1.8 t) \hat{\mathrm{i}} \mathrm{N}$ (with $t$ in seconds) is applied to the box. The acceleration of the box as a function of time $t$ is given by $\vec{a}=0$ for $0 \leq t \leq 2.8 \mathrm{~s}$ and $\vec{a}=(1.2 t-2.4) \hat{i} \mathrm{~m} / \mathrm{s}^{2}$ for $t>2.8 \mathrm{~s}$. (a) What is the coefficient of static friction between the box and the surface? (b) What is the coefficient of kinetic friction between the box and the surface?

94 A child weighing 140 N sits at rest at the top of a playground slide that makes an angle of $25^{\circ}$ with the horizontal. The child keeps from sliding by holding onto the sides of the slide. After letting go of the sides, the child has a constant acceleration of $0.86 \mathrm{~m} / \mathrm{s}^{2}$ (down the slide, of course). (a) What is the coefficient of kinetic friction between the child and the slide? (b) What maximum and minimum values for the coefficient of static friction between the child and the slide are consistent with the information given here?

95 In Fig. 6-61 a fastidious worker pushes directly along the handle of a mop with a force $\vec{F}$. The handle is at an angle $\theta$ with the vertical, and $\mu_{s}$ and $\mu_{k}$ are the coefficients of static and kinetic friction between the head of the mop and the floor. Ignore the mass of the handle and assume that all the mop's mass $m$ is


Fig. 6-61 Problem 95.
in its head. (a) If the mop head moves along the floor with a constant velocity, then what is $F$ ? (b) Show that if $\theta$ is less than a certain value $\theta_{0}$, then $\vec{F}$ (still directed along the handle) is unable to move the mop head. Find $\theta_{0}$.
96 A child places a picnic basket on the outer rim of a merry-goround that has a radius of 4.6 m and revolves once every 30 s . (a) What is the speed of a point on that rim? (b) What is the lowest value of the coefficient of static friction between basket and merry-go-round that allows the basket to stay on the ride?
97 SSM A warehouse worker exerts a constant horizontal force of magnitude 85 N on a 40 kg box that is initially at rest on the horizontal floor of the warehouse. When the box has moved a distance of 1.4 m , its speed is $1.0 \mathrm{~m} / \mathrm{s}$. What is the coefficient of kinetic friction between the box and the floor?

98 In Fig. 6-62, a 5.0 kg block is sent sliding up a plane inclined at $\theta=37^{\circ}$ while a horizontal force $\vec{F}$ of magnitude 50 N acts on it. The coefficient of kinetic friction between block and plane is 0.30 . What are the (a) magnitude and (b) direction (up or down the plane) of the block's acceleration? The block's initial speed is 4.0 $\mathrm{m} / \mathrm{s}$. (c) How far up the plane does the block go? (d) When it reaches its highest point, does it remain at rest or slide back down the plane?


Fig. 6-62 Problem 98.

** View All Solutions Here **

## www.meetyourbrain.com

Ask questions get answers, homework help

Chapter 6

| Question No. | The answer |  |
| :---: | :---: | :---: |
| 1 | $\mathbf{C}$ |  |
| 2 | A |  |
| 3 | A |  |
| 4 | D |  |
| 5 | A |  |
| 6 | $\mathbf{B}$ |  |
| 7 | A |  |
| 8 | B |  |
| 9 | A |  |
| 10 | $\mathbf{B}$ |  |

## Chapter 6: FORCE AND MOTIN II

1. In the figure a woman pulls a loaded sled of mass $\mathbf{m}$ along a horizontal surface at constant velocity. The coefficient of kinetic friction between the runners and the snow is $\mu_{\mathbf{k}}$.
Which figure shows the correct free body diagram for the sled and load?

(a)

(b)

(c)

(d)

2. In question 2 , The equation of the forces acting on the load and sled (from Newton's second law) is:
(a) $\bar{T}+\vec{N}+\vec{F}_{g}+\vec{f}_{k}=0$
(b) $\vec{T}+\vec{N}+\vec{F}_{g}+\vec{f}_{s}=0$
(c) $\vec{T}+\vec{N}+\vec{F}_{g}+\vec{f}_{k}=m \vec{a}$
(d) $\vec{T}+\vec{N}+\vec{F}_{g}+\vec{f}_{s}=m \vec{a}$
3. A $12 \mathbf{N}$ horizontal force pushes a block of weight $5 \mathbf{N}$ to make it move with constant speed, the value of the coefficient of friction $\mu_{k}$ is:
(a) 2.4
(b) 0.24
(c) 4.1
(d) 0.41
4. A car has a weight of $\mathbf{1 . 1 ~ \mathbf { N }}$ slides on the road with acceleration $\mathbf{a}=\mathbf{1 . 2 4} \mathbf{~ m} / \mathbf{s}^{\mathbf{2}}$, what is the force of friction between the car and the road?
(a) -1.13 N
(b) -11 N
(c) -1.4 N
(d) -0.14 N
5. A $12 \mathbf{N}$ horizontal force pushes a block of weight $5 \mathbf{N}$ to make it move with constant speed, the value of the coefficient of friction $\mu_{k}$ is:
(a) 2.4
(b) 0.24
(c) 4.1
(d) 0.41

6. A block lies on a floor. If the maximum value $f_{\mathbf{x}, \max }$ of the static frictional force on the block is $\mathbf{1 0} \mathbf{N}$, what is the magnitude of the frictional force if the magnitude of the horizontally applied force is $\mathbf{8} \mathbf{N}$ ?
(a) 10 N
(b) 8 N
(c) 2 N
(d) 18 N
7. A $470 \mathbf{N}$ horizontal force pushes a block of mass $79 \mathbf{k g}$ to make it move with constant speed, what is the value of the coefficient of friction $\mu_{k}$ ?
(a) 0.61
(b) 6
(c) 1.6
(d) 0.06
8. A block lies on a floor.If the maximum value $f_{\mathbf{x}, \max }$ of the static frictional force on the block is $\mathbf{1 0} \mathbf{N}$, what is the magnitude of the frictional force if the magnitude of the horizontally applied force is $\mathbf{1 2} \mathbf{N}$ ?
(a) 10 N
(b) 12 N
(c) 2 N
(d) 22 N
9. In the figure, block B weighs $711 \mathbf{N}$. The coefficient of static friction between the block and the table is $\mathbf{0 . 2 5}$ assume that the cord between B and the knot is horizontal

What is the magnitude of the tension $T$ ?

(a) 205.2 N
(b) 355.5 N
(c) 820.1 N
(d) 1422 N
10. In question 9, the weight of block $\mathbf{A}$ is :
(a) $\mathrm{T} \cos 30$
(b) $\mathrm{T} \sin 30$
(c) $\mathrm{F}_{\mathrm{g}}-\mathrm{T} \cos 30$
(d) $F_{g}-T \sin 30$

CH 6


 - ís - C 0 した -


(a) (a)
$3 \quad F_{\text {Net }}=m a$
$F-\mu_{k} F_{N}=0 \Rightarrow 12-\mu_{k} m g=0$
$12-\mu_{k} \stackrel{\pi}{5}=0$


$$
\mu_{k}=\frac{12}{5}=2.4
$$

 . $6 ; 00 \mathrm{mg}$

$4 \xrightarrow{f_{k} \text { —o }}$


$$
\begin{aligned}
F_{N e t} & =m a \\
\Theta F_{k} & =m a \\
& =-(0.1122 \times 1.24)=-0.139 \mathrm{~N}
\end{aligned}
$$

$$
\begin{aligned}
& w=m g=1.1 \\
& m=\frac{1.1}{9.8}=0.1122
\end{aligned}
$$



CH6 2 ゼ

． $f_{s}=F \quad$ S $i$ í is lm mul ine $f_{s}$



：
（1）

$$
\begin{aligned}
& f_{5 \max }=10 \mathrm{~N} \\
& F=3 \mathrm{~N}
\end{aligned}
$$

$$
\begin{gathered}
f_{5 \text { max }}=10 \mathrm{~N} \\
F=12 \mathrm{~N}
\end{gathered}
$$


㑔 F F ن



$$
f_{s}=F \quad \text { iv isw } \alpha \text { ! k }
$$

$$
F_{5}=8 \mathrm{~N}
$$



Nows cl Libsion or

 Pixócula ás ibsioul F，
 uscll is jen：

$7-$

$$
\begin{gathered}
F_{N e t}=m a \\
F-\mu_{k} F_{N}=0 \\
470-\mu_{k}(79 \times 9.8)=0 \\
\mu_{k}=0.607
\end{gathered}
$$

CH 6 er




$$
\begin{aligned}
& F_{\text {Net }}=m a \\
& (T \cos \theta)-f_{s}=0 \\
& \mu_{s} F_{N} \\
& (0.25)(\mathrm{mg})
\end{aligned}
$$

$$
\begin{aligned}
& T \cos \theta-177.5=0 \\
& T \frac{\cos 30}{\cos 30}=\frac{177.5}{\cos 30} \\
& T=205.2
\end{aligned}
$$




## Chapter 6

## Force and Motion - II

6-1

In this chapter, we will study two types of forces: friction force and centripetal force.

## 6-2 Friction There are two types of friction force:

## 1- static friction force

2- kinetic friction forces

(e) The block is accelerating in direction of $F$. The block slides along the surface. The friction force is called kinetic friction force
(f) The block moves at constant velocity


FIG. 6-1 (a) The forces on a stationary block. ( $b-d$ ) An external force $\vec{F}$, applied to the block, is balanced by a static frictional force $\vec{f}_{3}$. As $F$ is increased, $f_{s}$ also increases, until $f_{s}$ reaches a certain maximum value. (e) The block then "breaks away," accelerating suddenly in the direction of $\vec{F}$. ( $f$ ) If the block is now to move with constant velocity, $F$ must be reduced from the maximum value it had just before the block broke away. (g) Some experimental results for the sequence $(a)$ through $(f)$.

## 6-3 Properties of Friction

Property 1. If the body does not move, then the static frictional force $\vec{f}$ s and the component of $\vec{F}$ that is parallel to the surface balance each olher. They are equal in magnitude, and $\vec{f}_{s}$ is directed opposite that component of $\vec{F}$.

- Property 2. The magnitude of $\vec{f}_{s}$ has a maximum value $f_{s, \text { max }}$ that is given by

$$
f_{s, \text { max }}=\mu_{s} F_{N},
$$

where $\mu_{s}$, is the cocfficient of static friction and $F_{N}$ is the magnitude of the normal force on the body from the surface. If the magnitude of the component of $F$ that is parallel to the surface exceeds f,max, then the body begins to slide along the surface.
Property 3. If the body begins to slide along the surface, the magnitude of the frictional force rapidly decreases to a value $f_{k}$ given by

$$
\begin{equation*}
f_{k}=\mu_{k} F_{N}, \tag{6-2}
\end{equation*}
$$

where $\mu_{k}$ is the coefficient of kinctic friction. Thereafter, during the sliding, a kinelic frictional force $\vec{f}_{k}$ with magnitude given by Eq. 6-2 opposes the motion.

The coefficients $\mu_{s}$ and $\mu_{k}$ are dimensionless and must be determined experimentally. Their values depend on certain properties of both the body and the surface

CHECKPOINT 1 A block lies on a floor. (a) What is the magnitude of the frictional force on it from the floor? (b) If a horizontal force of 5 N is now applied to the block, but the block does not move, what is the magnitude of the frictional force on it? (c) If the maximum value $f_{s, \max }$ of the static frictional force on the block is 10 N , will the block move if the magnitude of the horizontally applied force is 8 N ? (d) If it is 12 N ? (e) What is the magnitude of the frictional force in part (c)?

Answer: (a) zero (b) 5 N (c) no (d) yes (e) 8 N

If a car's wheels are "locked" (kept from rolling) during


Ripped-off bits of tire and small melted sections of road form the "skid marks" that reveal that cold-welding occurred during the slide. The record for the longest skid marks on a public road was reportedly set in 1960 by a Jaguar on the M1 highway in England (Fig. 6-3a) the marks were 290 m long! Assuming that $\mu_{k}=0.60$ and the car's acceleration was constant during the braking, how fast was the car going when the wheels became locked?

Answer: To find the car's initial speed, we can use the constant acceleration equation because the acceleration is constant

$$
\begin{gathered}
v^{2}=v_{0}^{2}+2 a\left(x-x_{0}\right) \\
-f_{k}=m a \\
a=-\frac{f_{k}}{m}=-\frac{\mu_{k} m g}{m}=-\mu_{k} g_{9} \\
=(-0.6)(9.8)=-5.88 \mathrm{~m} / \mathrm{s}^{2}
\end{gathered}
$$

Acceleration is in negative direction of $x$ axis

## Sample Problem 6-2

In Fig. $6.4 a$, a block of mass $m=3.0 \mathrm{~kg}$ slides along a floor while a force $\vec{F}$ of magnitude 12.0 N is applied to it at an upward angle $\theta$. The coefficient of kinetic friction between the block and the floor is $\mu_{k}=0.40$.

(a)

What is the acceleration of the block?

## 6-5 Uniform Circular Motion

From Section 4.7, recall that when a body moves in a circle (or a circular arc) at constant speed $v$, it is said to be in uniform circular motion. Also recall that the body has a centripetal acceleration (directed toward the center of the circle) of constant magnitude given by

$$
\begin{equation*}
a=\frac{v^{2}}{R} \quad \text { (centripetal acceleration) } \tag{6-17}
\end{equation*}
$$

where $R$ is the radius of the circle.
We have three exampl es
1- Rounding a curve in a car: in this situation, centripetal force is frictional force on the tires from the road


2- Orbiting Earth: in this situation, cetripetal force is gravity force


3- Hockey Puck: in thi situation, centripetal force on the puck is tension


A centripetal force accelerates a body by changing the direction of the body's velocity without changing the body's speed.

From Newton's second law and Eq. 6-17 $\left(a=v^{2} / R\right)$, we can write the magnitude $F$ of a centripetal force (or a net centripetal force) as

$$
\begin{equation*}
F=m \frac{v^{2}}{R} \quad \text { (magnitude of centripetal force). } \tag{6-18}
\end{equation*}
$$

Because the speed $v$ here is constant, the magnitudes of the acceleration and the force are also constant.

CHECKPOINT 2 When you ride in a Ferris wheel at constant speed, what are the directions of your acceleration $\vec{a}$ and the normal force $\vec{F}_{N}$ on you (from the always upright seat) as you pass through (a) the highest point and (b) the lowest point of the ride?

## Answer: (a) a downward, $\mathrm{F}_{\mathrm{N}}$ upward (b) a and $\mathrm{F}_{\mathrm{N}}$ upward

## Sample Problem 6-6

Igor is a cosmonaut on the International Space Station, in a circular orbit around Earth, at an altitude $h$ of 520 km and with a constant speed $v$ of $7.6 \mathrm{~km} / \mathrm{s}$. Igor's mass $m$ is 79 kg .
(a) What is his acceleration?

## Answer:

$R_{E}$ is Earth's radius $\left(6.37 \times 10^{6} \mathrm{~m}\right.$,

$$
\begin{aligned}
a & =\frac{v^{2}}{R}=\frac{v^{2}}{R_{E}+h} \\
& =\frac{\left(7.6 \times 10^{3} \mathrm{~m} / \mathrm{s}\right)^{2}}{6.37 \times 10^{6} \mathrm{~m}+0.52 \times 10^{6} \mathrm{~m}} \\
& =8.38 \mathrm{~m} / \mathrm{s}^{2} \approx 8.4 \mathrm{~m} / \mathrm{s}^{2}
\end{aligned}
$$

(Answer)
(b) What force does Earth exert on Igor?

$$
\begin{align*}
F_{g} & =m a=(79 \mathrm{~kg})\left(8.38 \mathrm{~m} / \mathrm{s}^{2}\right) \\
& =662 \mathrm{~N} \approx 660 \mathrm{~N} . \tag{Answer}
\end{align*}
$$

