Jeddah University

PHYSICS (101)

Chapter (3)
Motion in two dimensions

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Position and Velocity Vectors

Example 1:

A particle moving from $\vec{r_1} = 2\hat{i} + 5\hat{j} + 8\hat{k}$ to $\vec{r_2} = 12\hat{i} + 10\hat{j} + 8\hat{k}$, then the displacement is:

Solution:

(A) $10\hat{i} - 3\hat{j}$
(B) $4\hat{i} + 6\hat{j}$
(C) $10\hat{i} + 5\hat{j}$
(D) $5\hat{j}$

(C)

$$\Delta r = r_2 - r_1$$

$$\Delta r = 12i + 10j + 8k - (2i + 5j + 8k)$$

$$= 12i + 10j + 8k - 2i - 5j - 8k$$

$$= 10i + 5j$$ ✓

Position and Velocity Vectors (2)

Example 2:

A particle moves in xy plane as $x(t) = 2t\ (m)$ and $y(t) = t^2 - 1\ (m)$. The velocity of the particle at t=1 s is:

Solution:

(D)

(A) $\hat{i} + \hat{j}$ (m/s)
(B) $2\hat{i} + \hat{j}$ (m/s)
(C) $2\hat{i} - \hat{j}$ (m/s)
(D) $2\hat{i} + 2\hat{j}$ (m/s)

$x = 2t$

$v_x = 2$

$v_x = 2$

$y = t^2 - 1$

$v_y = 2t$

$v_y = 2 \times 1 = 2$

$v = 2i + 2j$ m/s

The Acceleration Vector (3)

Example 3:

At t=0, a car moves with velocity $\overrightarrow{v_0} = 2\hat{i} + \hat{j}$ (m/s) and acceleration $\vec{a} = 2\hat{j}$ (m/s^2). The velocity of the car at t=2 is:

Solution:

(A) $6\hat{i} + \hat{j}$
(B) $2\hat{i} + 5\hat{j}$
(C) $2\hat{i} + \hat{j}$
(D) $\hat{i} + 5\hat{j}$

(B)

$$v = v_0 + at$$

$$v = 2i + j + 2(2j)$$
$$= 2i + j + 4j$$
$$= 2i + 5j$$

(B)

Projectile Motion

Example 4:

A boy kicks a ball at an angle of 40^0 to the horizontal with speed of 14.0 m/s. The time it takes to reach the highest point is:

Solution:

$v_0 = 14$ m/s

$\theta = 40^\circ$

(A) $t = \dfrac{2v_0 \sin(\theta)}{g}$

$t = \dfrac{2 \times 14 \sin(40)}{9.8}$

$t = 1.84$ s (الزمن الكلي)

(A) 0.92 s

(B) 0.77 s

(C) 0.15 s

(D) 1.12 s

نصف الزمن $t = \dfrac{1.84}{2} = 0.92$

Projectile Motion

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Example 5:

A boy kicks a ball at an angle of 40^0 to the horizontal with speed of 14.0 m/s. The maximum height that the ball can reach is:

Solution:

(B)

$$H = \frac{v_0^2 \sin(\theta)^2}{2g}$$

$$H = \frac{14^2 \sin(40)^2}{2 \times 9.8}$$

$$H = 4.13 \text{ m}$$

(A) 9.87 m
(B) 4.13 m
(C) 15.33 m
(D) 12.68 m

B

Example 6:

Referring to question 5, the horizontal range that the ball can reach is:

Solution:

(A) 9.87 m
(B) 14.7 m
(C) 15.33 m
(D) 19.7 m

(D)

$$R = \frac{v_o^2 \sin(2\theta)}{g}$$

$$R = \frac{(14)^2 \sin(2 \times 40)}{9.8}$$

$$R = 19.7 \quad m$$

Projectile Motion

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Example 7:

A projectile is launched to achieve a maximum range of 140 m, the speed of the projectile must be:

Solution:

(A) 17 m/s
(B) 27 m/s
(C) 37 m/s
(D) 45 m/s

$\theta = 45^\circ$

(C) $R_{max} = 140\ m$

$$R_{max} = \frac{v_0^2}{g}$$

$$140 = \frac{v_0^2}{9.8} \qquad v_0 = 37\ m/s$$

Projectile Motion

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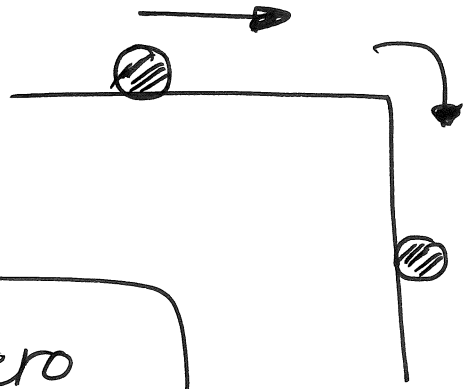
Example 8:

A toy car runs on a horizontal table with 3 m/s. The angle it makes with the horizontal when it leaves the table is:

Solution:

(A) Zero
(B) 45^0
(C) 60^0
(D) 90^0



Projectile Motion

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Example 9:

A stone is thrown horizontally from the top of a tall building. It follows a path that is:

Solution:

(D)

(A) circular
(B) two straight lines
(C) a straight line
(D) parabolic

Motion in a Circle

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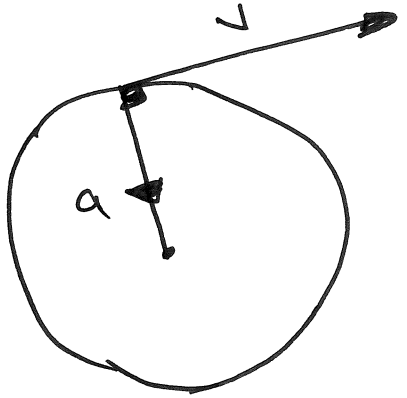
Example 10:

الحركة الدائرية المنتظمة التسارع السرعة

The velocity and acceleration of a body in a uniform circular motion are:

Solution:

(B)



(A) differed by 45^0

(B) perpendicular

(C) differed by 135^0

(D) parallel

Motion in a Circle

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Example 11:

A car rounds a 20 m radius curve at 10 m/s. The magnitude of its acceleration is:

Solution:

(A) zero
(B) 2 m/s^2
(C) 4 m/s^2
(D) 5 m/s^2

$R = 20 \quad m$

$U = 10 \quad m/s$

(D)

$$a = \frac{U^2}{R}$$

$$a = \frac{(10)^2}{20} = 5 \quad m/s^2$$

Motion in a Circle

(12)

Example 12:

A truck is traveling with a constant speed of 20 m/s. When the truck follows a curve in the road, its centripetal acceleration is 4.0 m/s^2. The radius of the curve is:

Solution:

(A) 225 m
(B) 144 m
(C) 100 m
(D) 81 m

(C)

$$a = \frac{v^2}{R}$$

$v = 20$ m/s

$a = 4$ m/s^2

$R = ?$

$$4 = \frac{(20)^4}{R}$$

$R = 100$ m

CH-3

* Example 3-1 ⟶ 69

$X = 2 - 0.25t^2$	$Y = t + 0.025t^3$
$X = 2 - 0.25(2)^2$	$Y = 2 + 0.025(2)^3$
$X = 1$	$Y = 2.2$

$$r = \sqrt{x^2 + y^2}$$

$$r = \sqrt{1^2 + (2.2)^2} = 2.4 \text{ m}$$

$$r = (2 - 0.25t^2)i + (t + 0.025t^3)j$$

at $t = 0$

$$r_1 = (2 - 0.25(0))i + (0 + 0.025 \times 0)j$$

$$r_1 = 2i$$

$t_2 = 2$

$$r_2 = (2 - 0.25(2)^2)j + (2 + 0.025(2)^3)j$$

$$r_2 = i + 2.2j$$

$$\Delta r = r_2 - r_1 = i + 2.2j - 2i$$

$$= -i + 2.2j$$

$$V_{ave} = \frac{\Delta r}{\Delta t} = \frac{-i + 2.2j}{2 - 0}$$

$$V_{ave} = -0.5i + 1.1j$$

* $V_{ave-x} = -0.5$ مركبة السرعة المتوسطة
* $V_{ave-y} = 1.1$

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* Example 3.6 ⟶ 78

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* $t = 0.50$ s

$X = v_{0x}t$

$X = 9 \times 0.50$

$X = 4.5$ m

$y = -\frac{1}{2}gt^2$

$= -\frac{1}{2} \times 9.8 \times (0.5)^2$

$= -1.2$ m

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* negative (below the starting point)
* distance at $t = 0.50$

$r = \sqrt{x^2 + y^2}$ $r = 4.7$ m

* at $t = 0.50$ s

* $v_x = v_{ox} = 9$ m/s

$v_y = v_{oy} + gt$

$v_y = 0 - 9.8 \times 0.5$

$v_y = -4.9$ m/s

* $v = v_x i + v_y j$

$v = 9i - 4.5j$

$v = \sqrt{v_x^2 + v_y^2}$

* $v = \sqrt{9^2 + (-4.9)^2} = 10.2$ m/s

* $\theta = \tan^{-1}\left(\frac{y}{x}\right)$

$\theta = \tan^{-1}\left(\frac{-4.9}{9}\right)$ $\theta = -29^\circ$

* Example 3.7

$v_0 = 37$ m/s

$\theta = 53.1^\circ$ $\quad t = 2$

$$v_{0x} = v_0 \cos(\theta)$$

$v_{0x} = 37 \cos(53.1)$

$= 22.2$ m/s

$$v_{0y} = v_0 \sin\theta$$

$v_{0y} = 37 \sin(53.1)$

$= 29.6$ m/s

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* $x = v_{0x} t = 22.2 \times 2 = 44.4$ m

* $$y = v_{0y} t + \frac{1}{2} g t^2$$

$= 29.6 \times 2 + \frac{1}{2} \times (-9.8) \times (2)^2 = 39.6$ m

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* $v_x = v_{0x} = 22.2$ m/s

* $$v_y = v_{0y} + gt$$

$v_y = 29.6 + (-9.8) \times 2 = 10$ m/s

$$v = \sqrt{v_x^2 + v_y^2}$$

$$v = \sqrt{22.2^2 + 10^2} = 24.2 \ m/s$$

* $\theta = \tan^{-1}\left(\frac{y}{x}\right)$

* $\theta = \tan^{-1}\left(\frac{10}{22.2}\right)$ $\quad \theta = 24.2^\circ$

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* Example: (3-12)

$$R = 5 \ m$$

$$T = 4 \ s$$

$$T = \frac{2\pi r}{v} \qquad v = \frac{2\pi r}{T}$$

$$v = \frac{2 \times 3.14 \times 5}{4}$$

$$v = 7.9 \ m/s$$

$$a = \frac{v^2}{R} \qquad a = \frac{7.9^2}{5} = 12 \ m/s^2$$